

KU LEUVEN

COST Action TU 1402 - Workshop 2
28-29 September 2015, Istanbul, Turkey

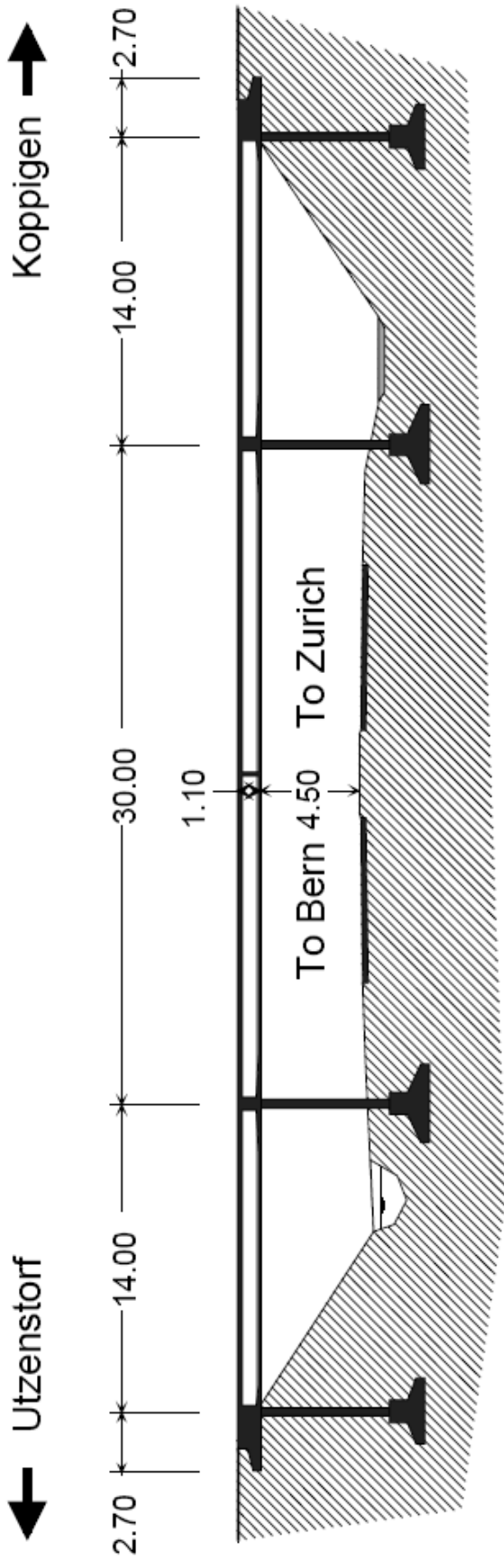
Fact sheet: monitoring the structural health of the Z24 bridge

Edwin Reynders, Eleni Chatzi
Michael Döhler and Geert Lombaert

KU Leuven - Department of Civil Engineering
ETH - Institut für Baustatik und Konstruktion
INRIA - Centre de recherche Rennes



The Z24 bridge benchmarks



- 3-span prestressed concrete highway bridge, built in 1963.
- Demolished in 1998 due to the construction of a railroad next to the highway.
- BE-3157 SIMCES (KU Leuven, Aalborg U., EMPA, LMS, Atkins, Sineco, TU Graz).
- One-year ambient vibration monitoring test, followed by a progressive damage test.
- Influence of environmental variations and realistic damage on modal characteristics.
- Long-term monitoring: natural frequencies (benchmark COST F3).
- Additional short-term monitoring during progressive damage test: natural frequencies, damping ratios, detailed mode shapes (benchmark IMAC XIX).

Overview of progressive damage test scenarios

1. Reference measurement (healthy structure).
2. Installation of lowering system.
- 3-6. Lowering of pier with 20, 40, 80, and 95mm (settlement, erosion).
7. Tilt of pier (settlement, erosion).



Overview of progressive damage test scenarios

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8. Reference measurement (lifting bridge to initial position).
- 9-10. Spalling of concrete over 12 and 24m² (vehicle impact, corrosion).
11. Landslide (erosion).

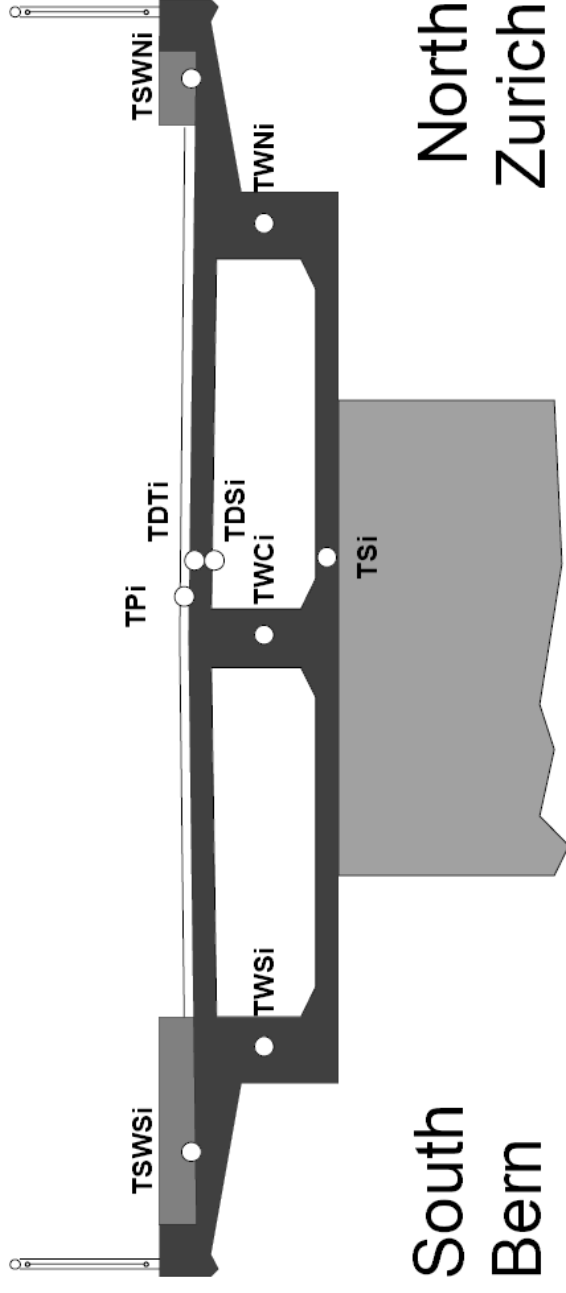


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11. Landslide (erosion).
12. Failure of concrete hinge (corrosion).
- 13-14. Failure of anchor heads (corrosion, overstress).
- 15-17. Rupture of tendons (corrosion).



Sensing technology



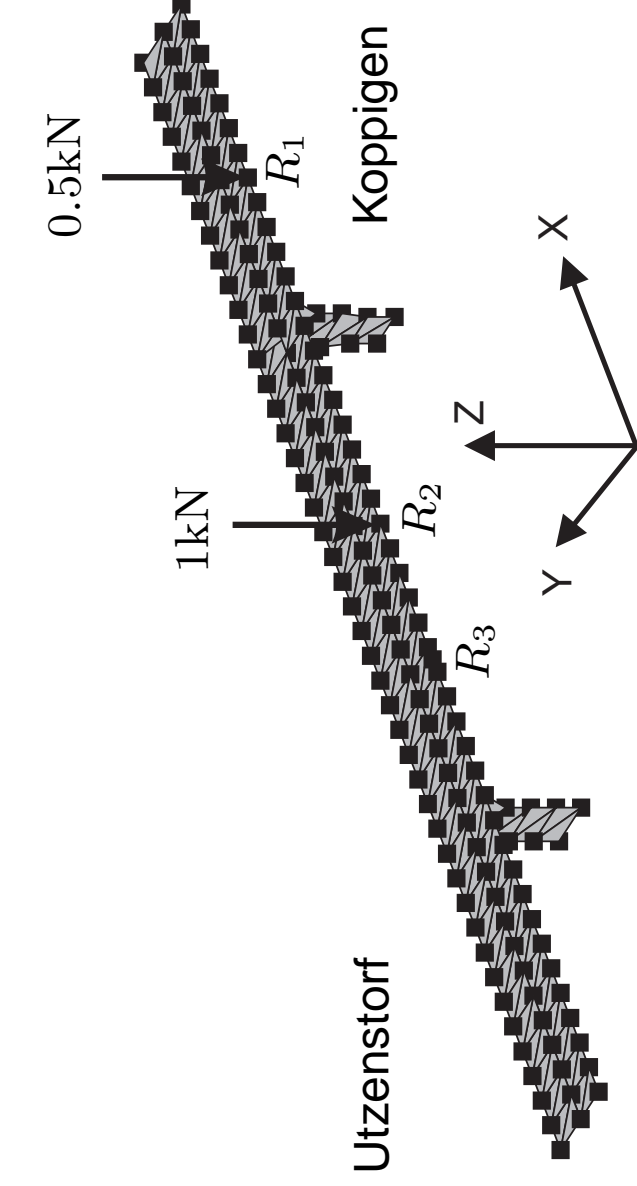
Long-term monitoring

- 5 sensors for atmospheric conditions, 1 sample/hour:
air temperature, air humidity, rain, wind speed, wind direction.
- 36 temperature sensors, 1 sample/hour.
- 7 static deformation sensors, 1 sample/hour.
- 16 accelerometers, 100 Hz, 11 min/hour.
- Automatic system identification for converting acceleration time series into natural frequency observations

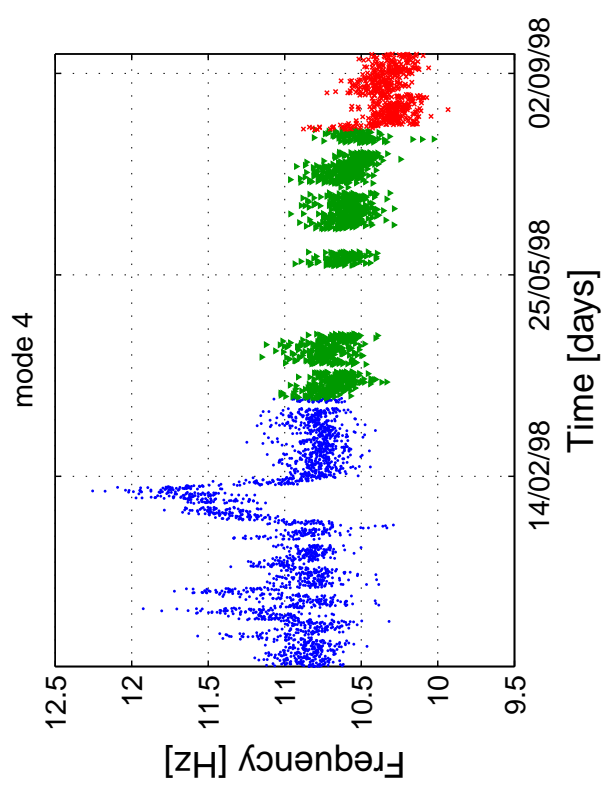
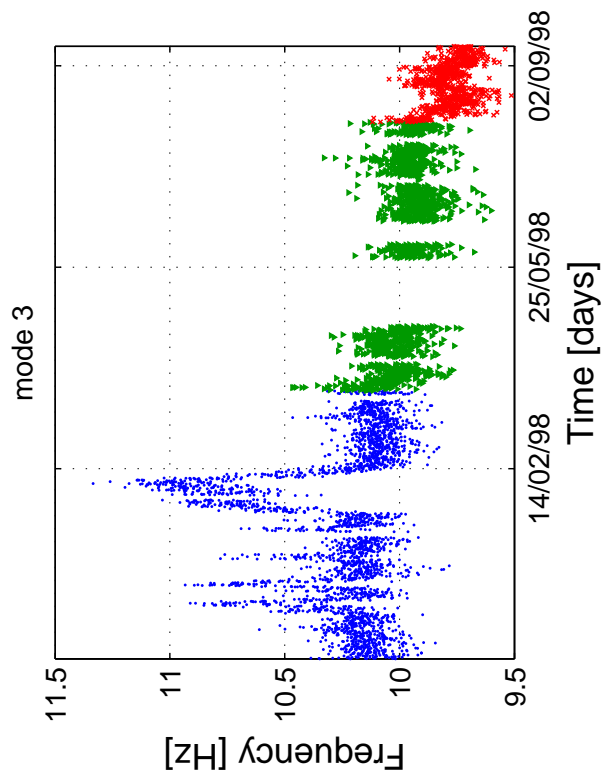
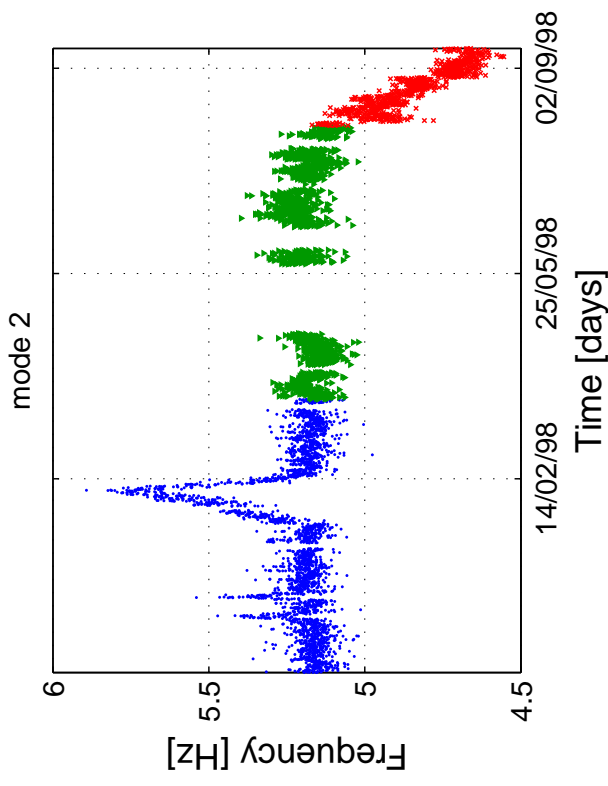
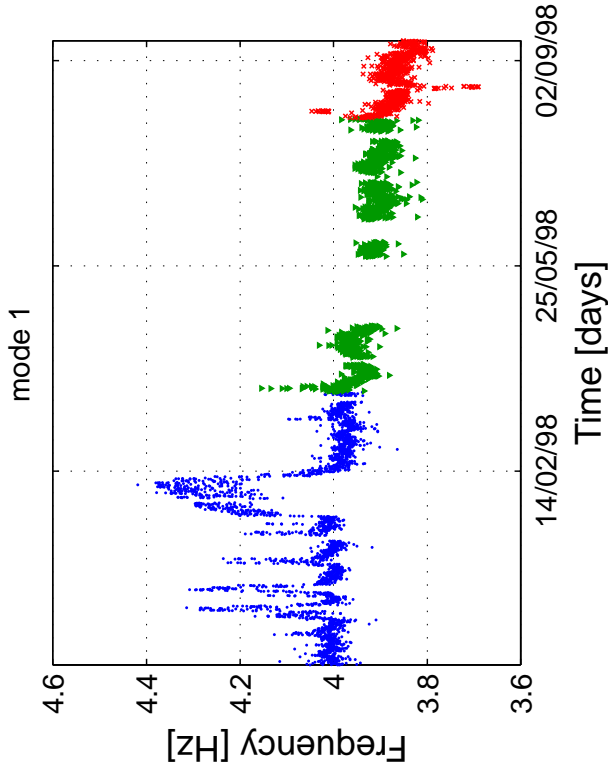
Additional short-term monitoring: sensing technology

Additional short-term monitoring

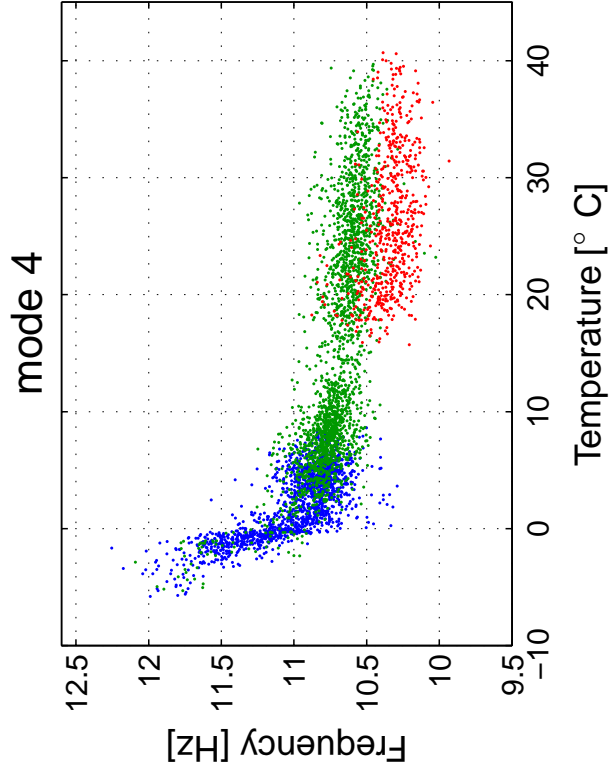
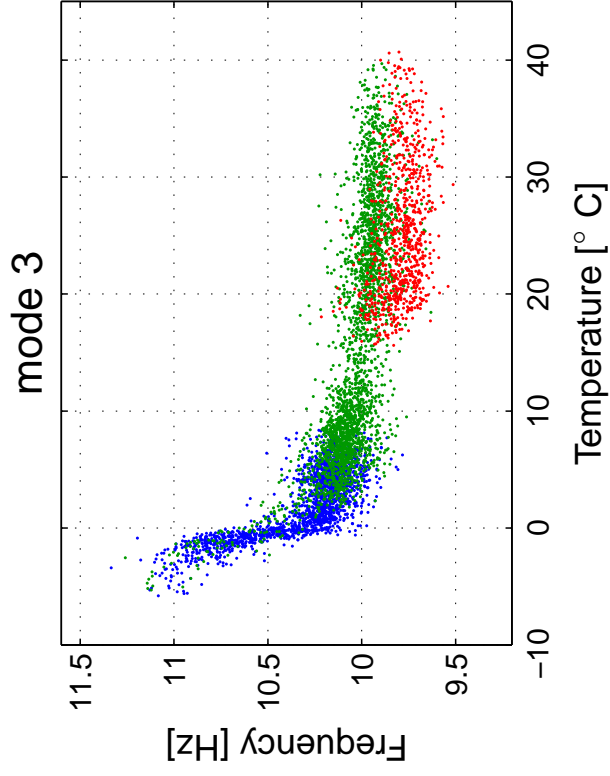
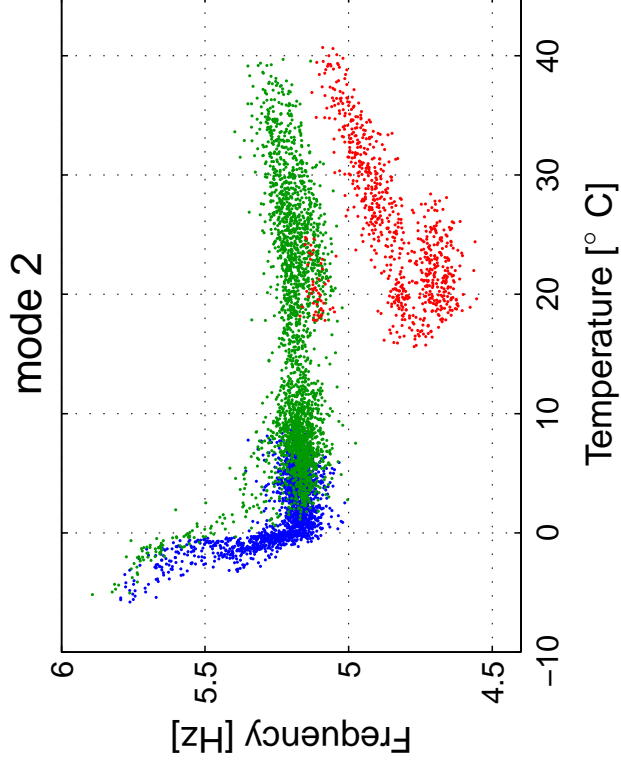
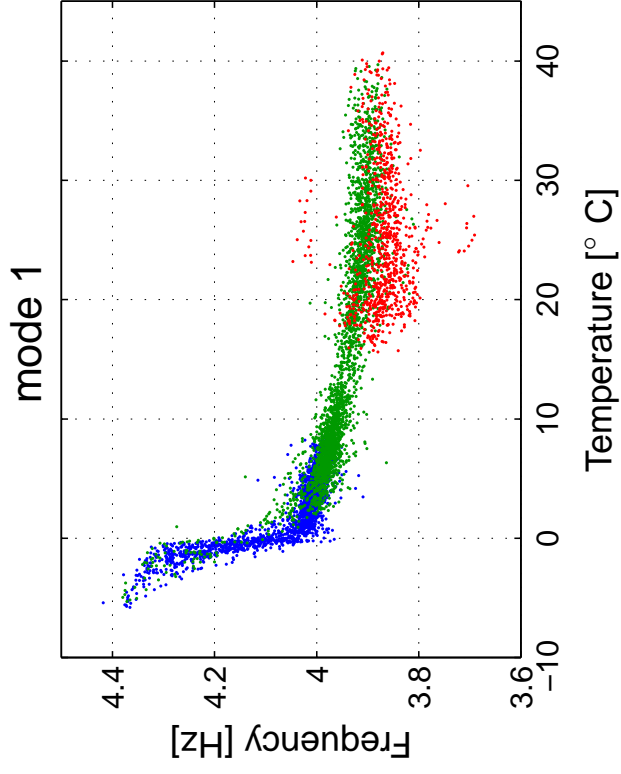
- Large-scale forced and ambient vibration test before and after each damage scenario.
- Outputs: 291 accelerations, 9 setups, 5 references.
- Shakers: 1kN at mid span, 0.5kN at side span, vertical, 3 – 30Hz



Long-term monitoring: observations



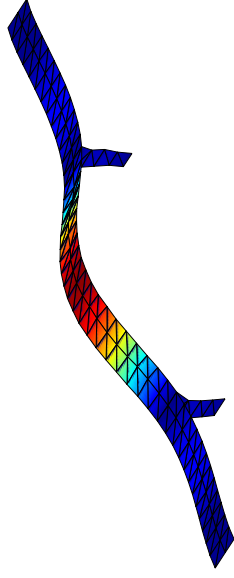
Long-term monitoring: observations



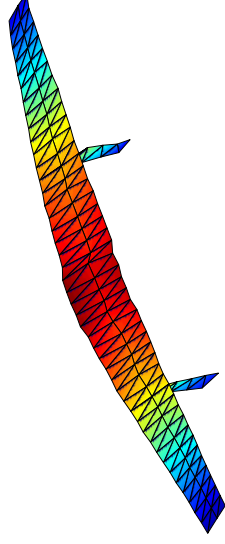
Additional short-term monitoring: observations

Ambient vibration test: 6 modes in between each applied damage case

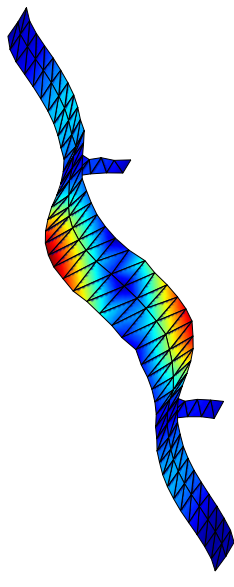
mode 1 - 3.86Hz - 0.8%



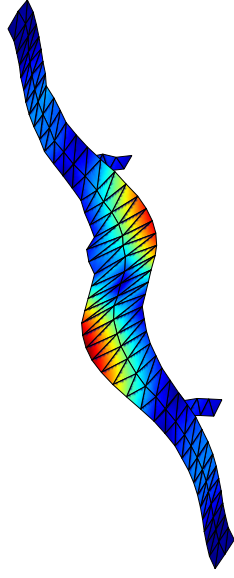
mode 2 - 4.90Hz - 1.4%



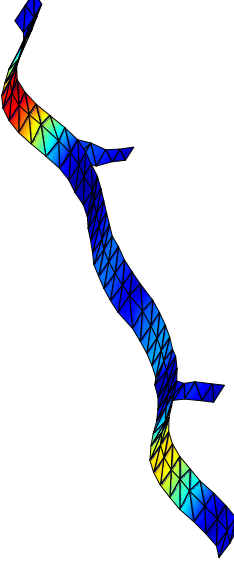
mode 3 - 9.76Hz - 1.4%



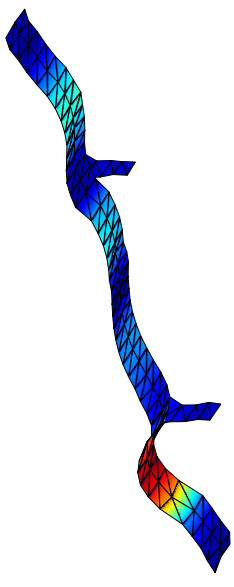
mode 4 - 10.30Hz - 1.3%



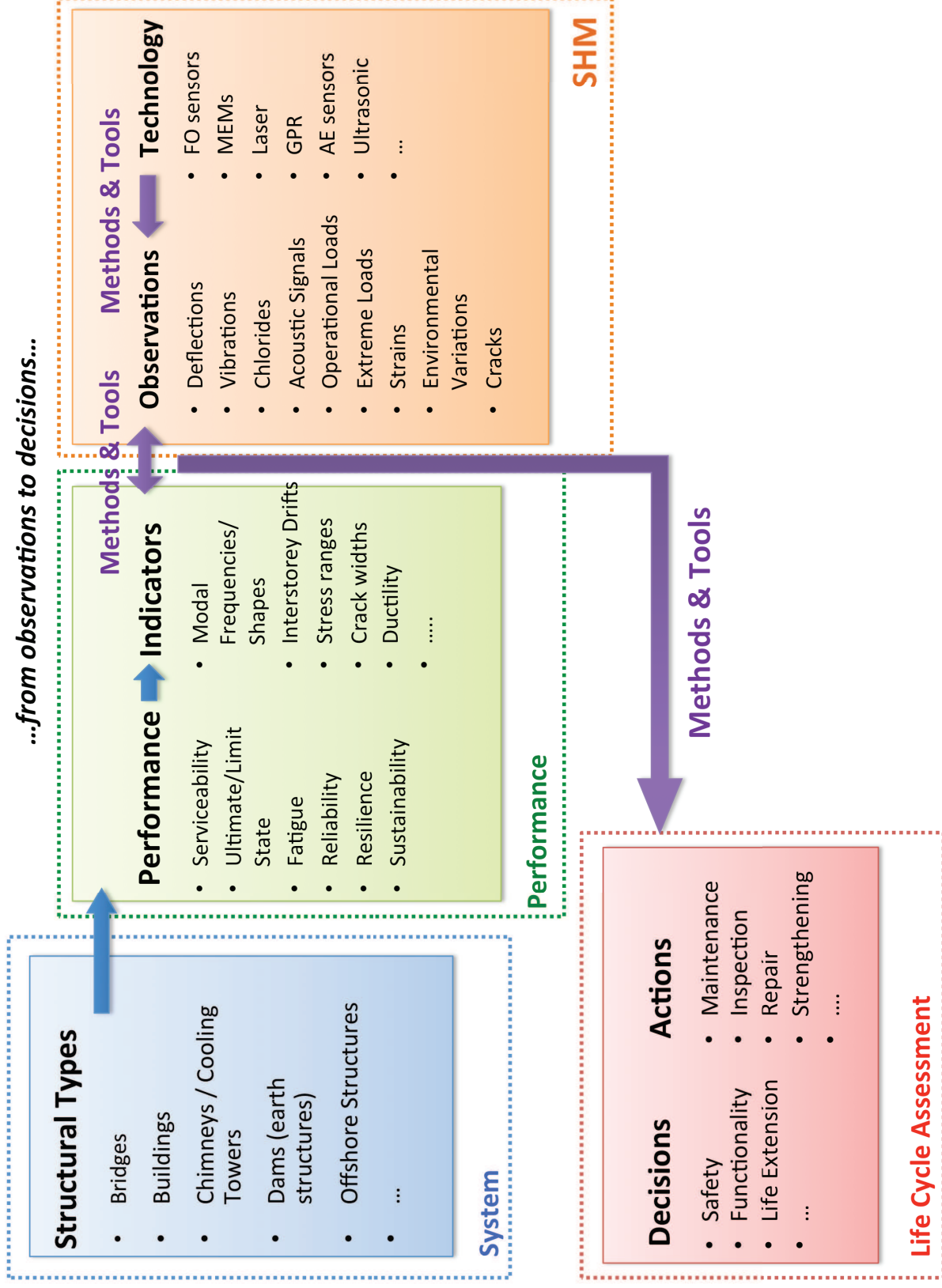
mode 5 - 12.41Hz - 2.8%



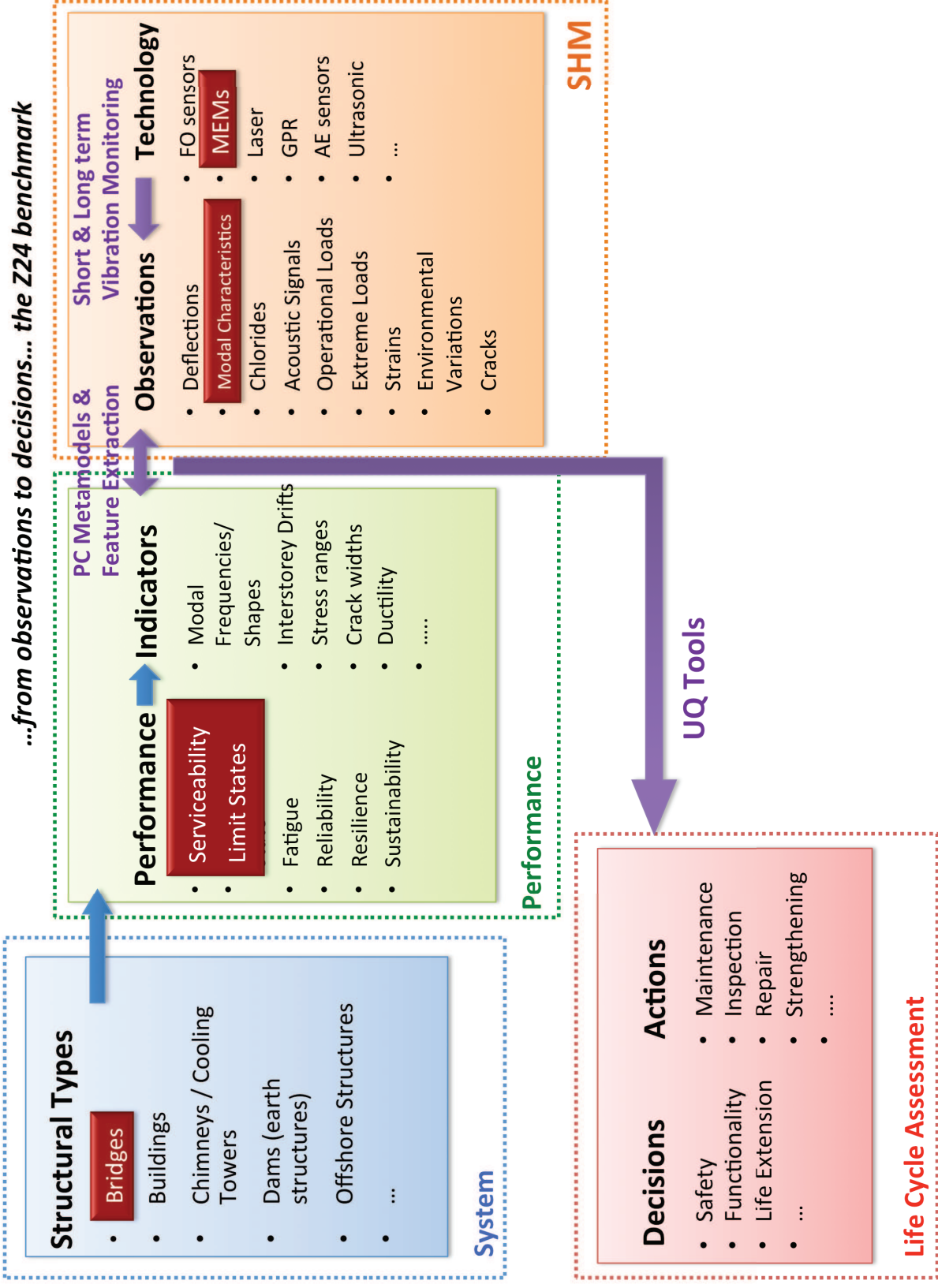
mode 6 - 13.25Hz - 3.2%



General framework

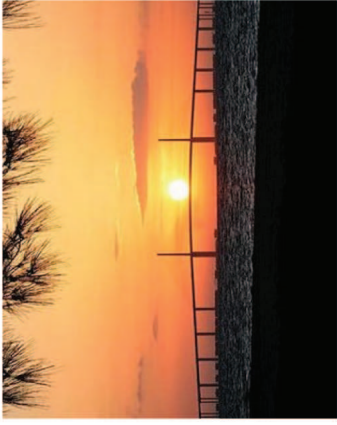
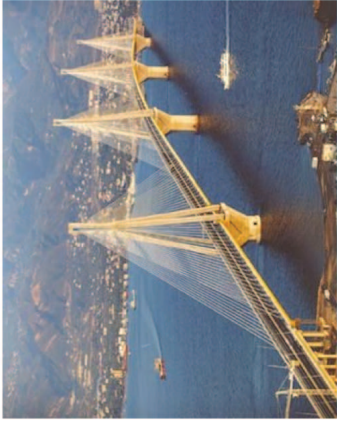


The Z24 bridge benchmarks



From long-term observations to performance indicators

Extraction of performance indicators based on ambient vibration response measurements.



Problem characteristics

Civil engineering structures are by default operating within continually changing environments.

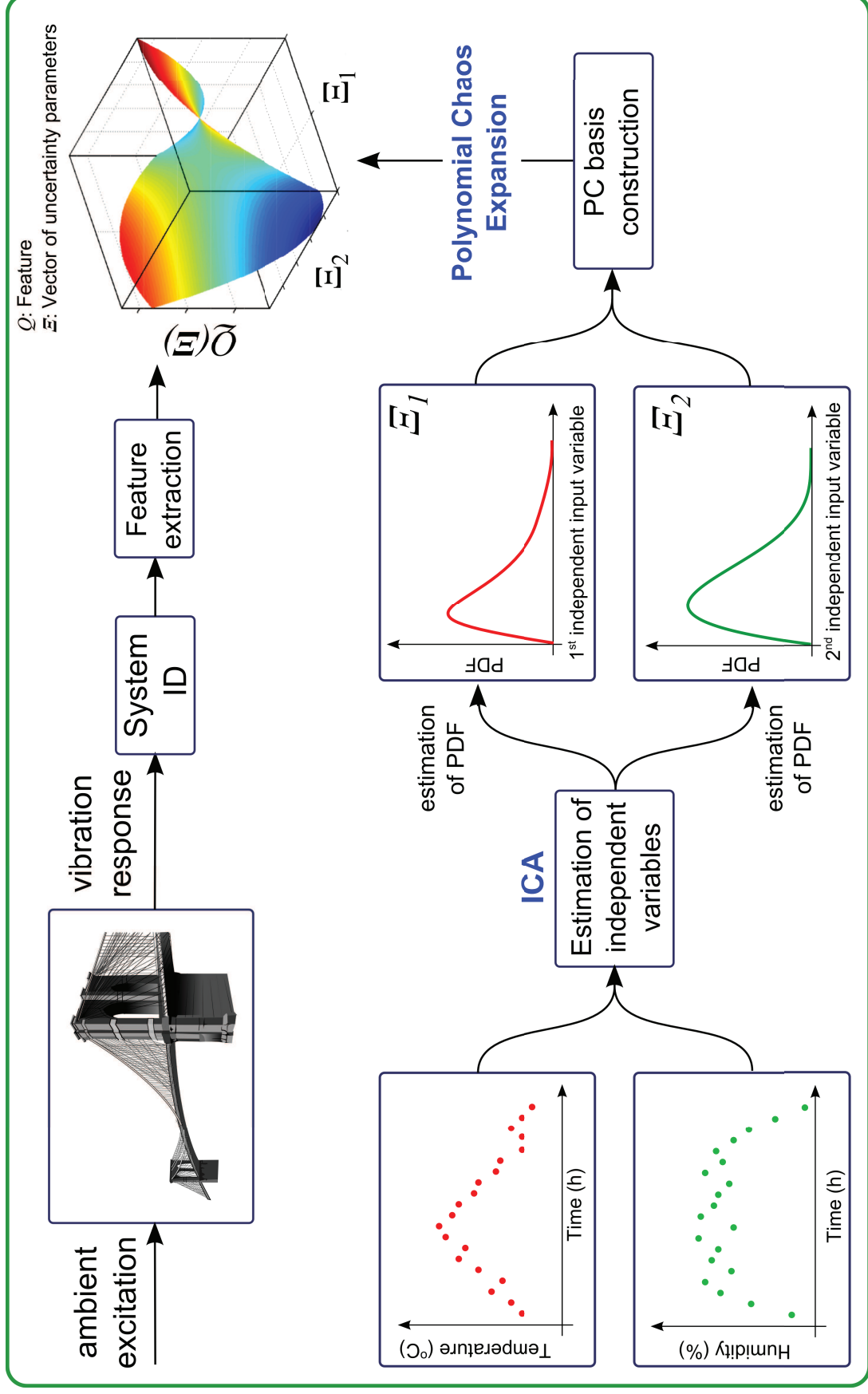
Environmental and other operating condition data should be incorporated into the structural ID framework.

Benefits of fusing operational condition data into structural ID

- Improved understanding of structural dynamics
- Improved design of new systems
- Improved Monitoring
- Condition Assessment
- Life – Cycle Management

From long-term observations to performance indicators

Stochastic Framework Structure



Polynomial Chaos Metamodels

Problem definition

Consider a system \mathcal{M} characterized by uncertain input parameters represented by independent random variables $\xi = [\xi_1, \xi_2, \dots, \xi_M]^T$ of prescribed probability density function $f(\xi)$. The **dynamic response of \mathcal{M}** to a given input excitation $x[t, \xi]$ will also be a **random variable**:

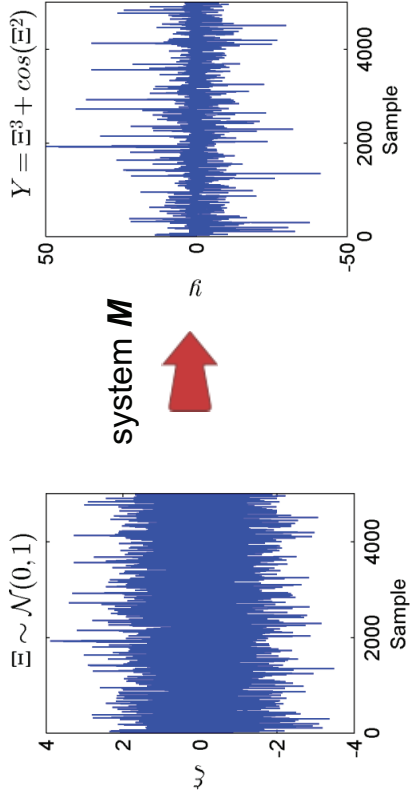
$$y[t, \xi] = \mathcal{M}(x[1, \xi], x[2, \xi], \dots, x[t, \xi], \xi), \quad t = 1, 2, \dots, T$$

The PC basis $\phi_{\alpha(j)}$ comprises polynomials that are orthonormal with respect to the joint probability density function of ξ . Assume the univariate case (single variable):

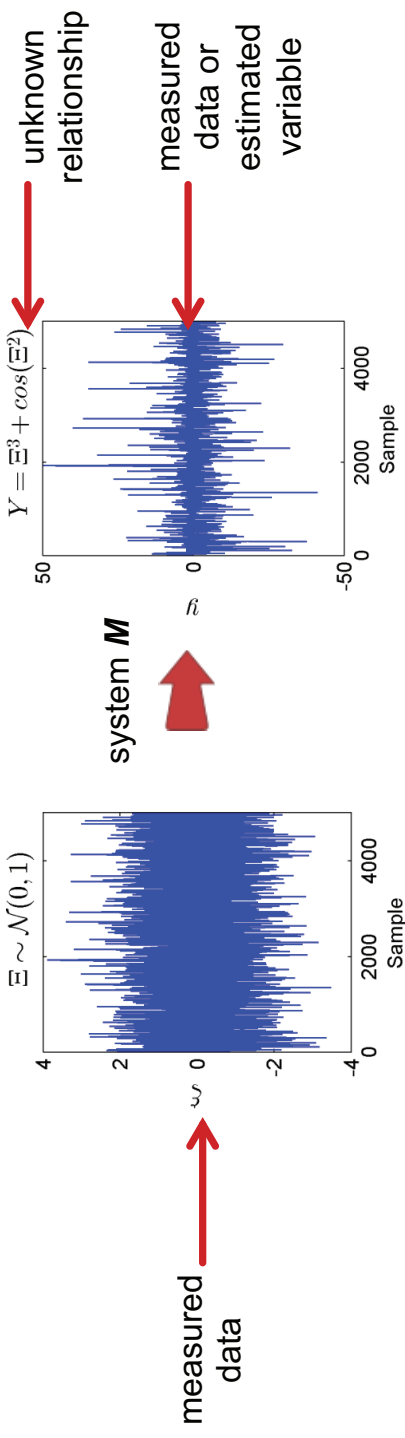
$$E[\phi_{\alpha}(\xi), \phi_{\beta}(\xi)] = \delta_{\alpha, \beta} = \begin{cases} 1 & \text{for } \alpha = \beta \\ 0 & \text{otherwise} \end{cases}$$

PDF	Support	Polynomials
Normal (Gaussian)	$(-\infty, \infty)$	Hermite
Uniform	$[-1, 1]$	Legendre
Gamma	$(0, 1)$	Laguerre
Chebyshev	$(-1, 1)$	Chebyshev
Beta	$(-1, 1)$	Jacobi

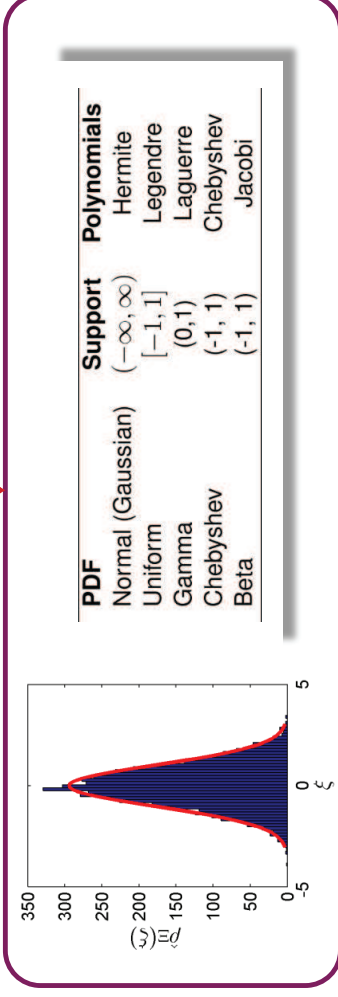
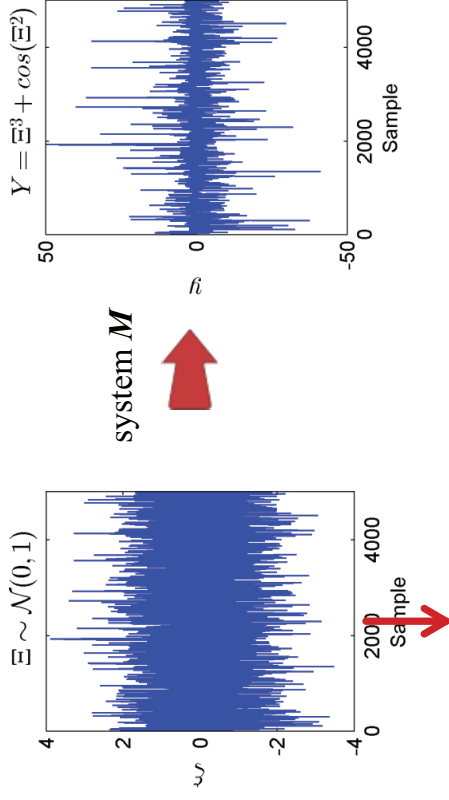
Polynomial Chaos Expansion



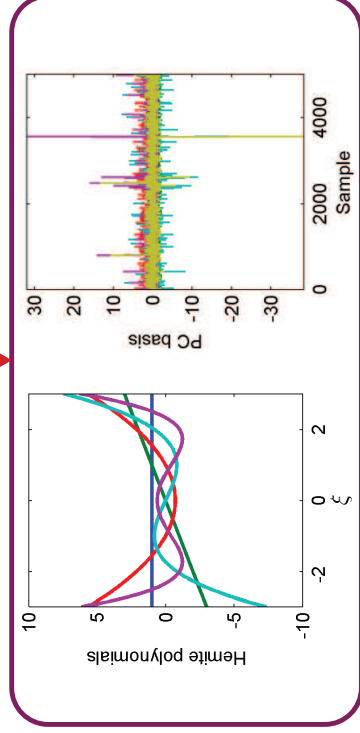
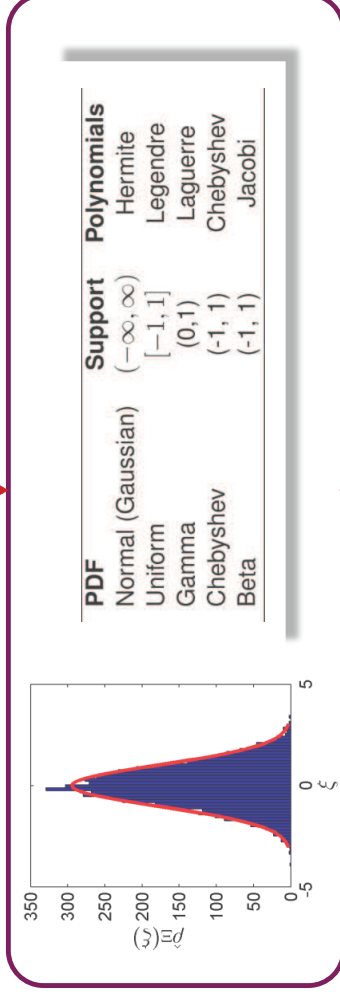
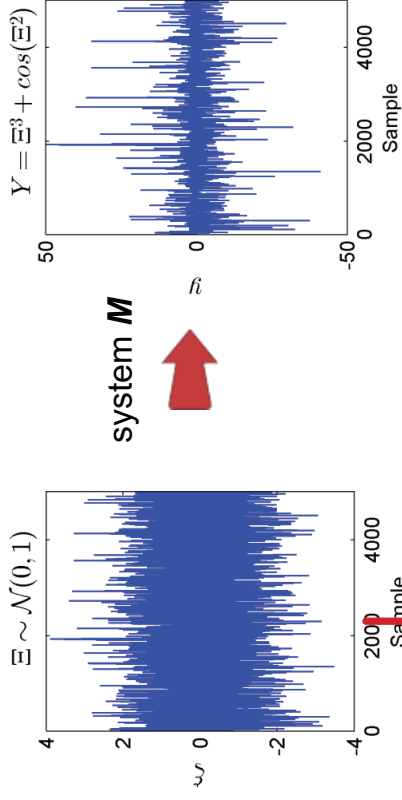
Polynomial Chaos Expansion



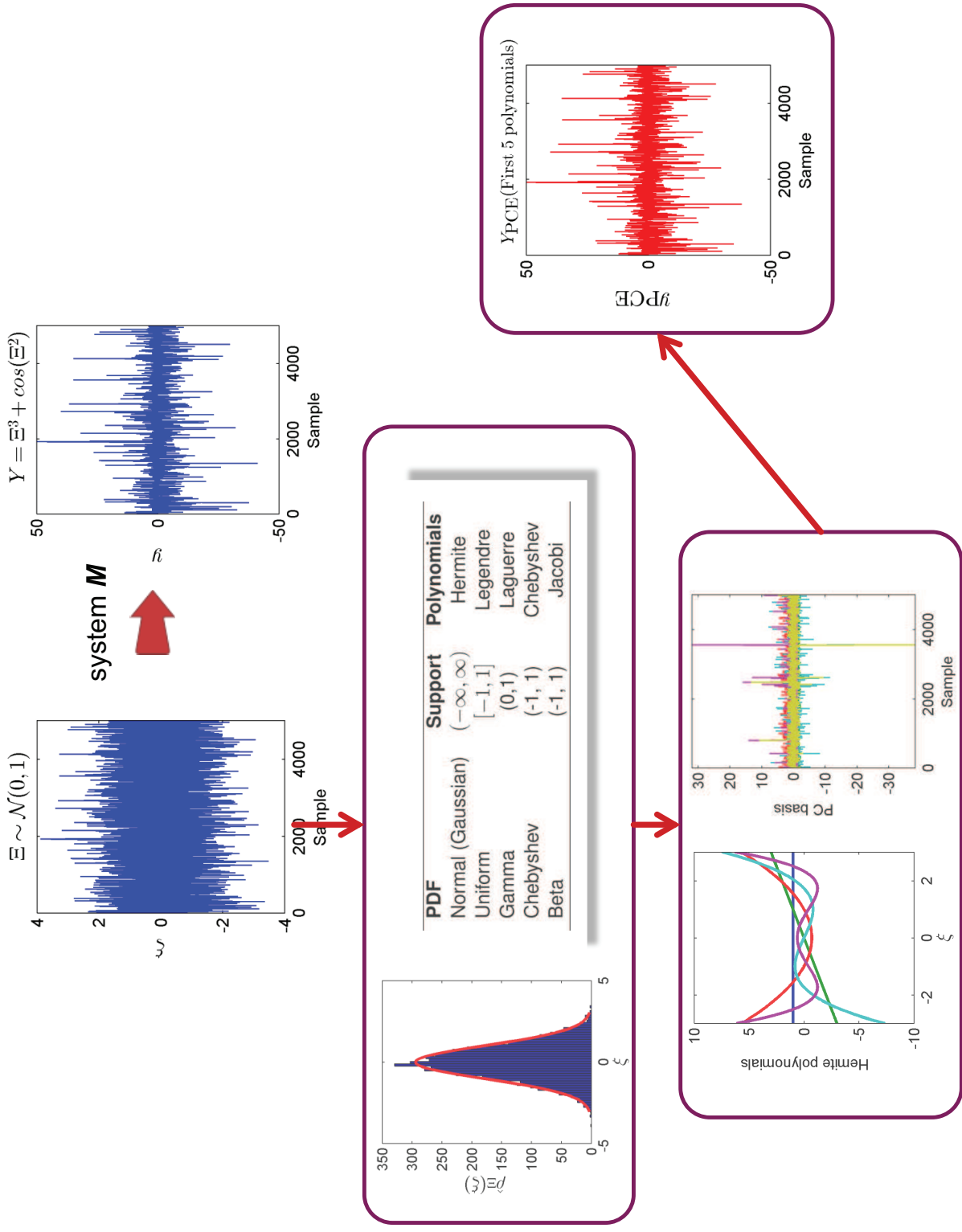
Polynomial Chaos Expansion



Polynomial Chaos Expansion



Polynomial Chaos Expansion



The ICA algorithm



Independent Component Analysis (ICA)

Allows for extraction of salient independent features.

Metamodel Prediction vs. Measurement

Multivariate Legendre polynomials of maximum order $P = 3$ used for the PC basis

ω_n

1

2

3

4

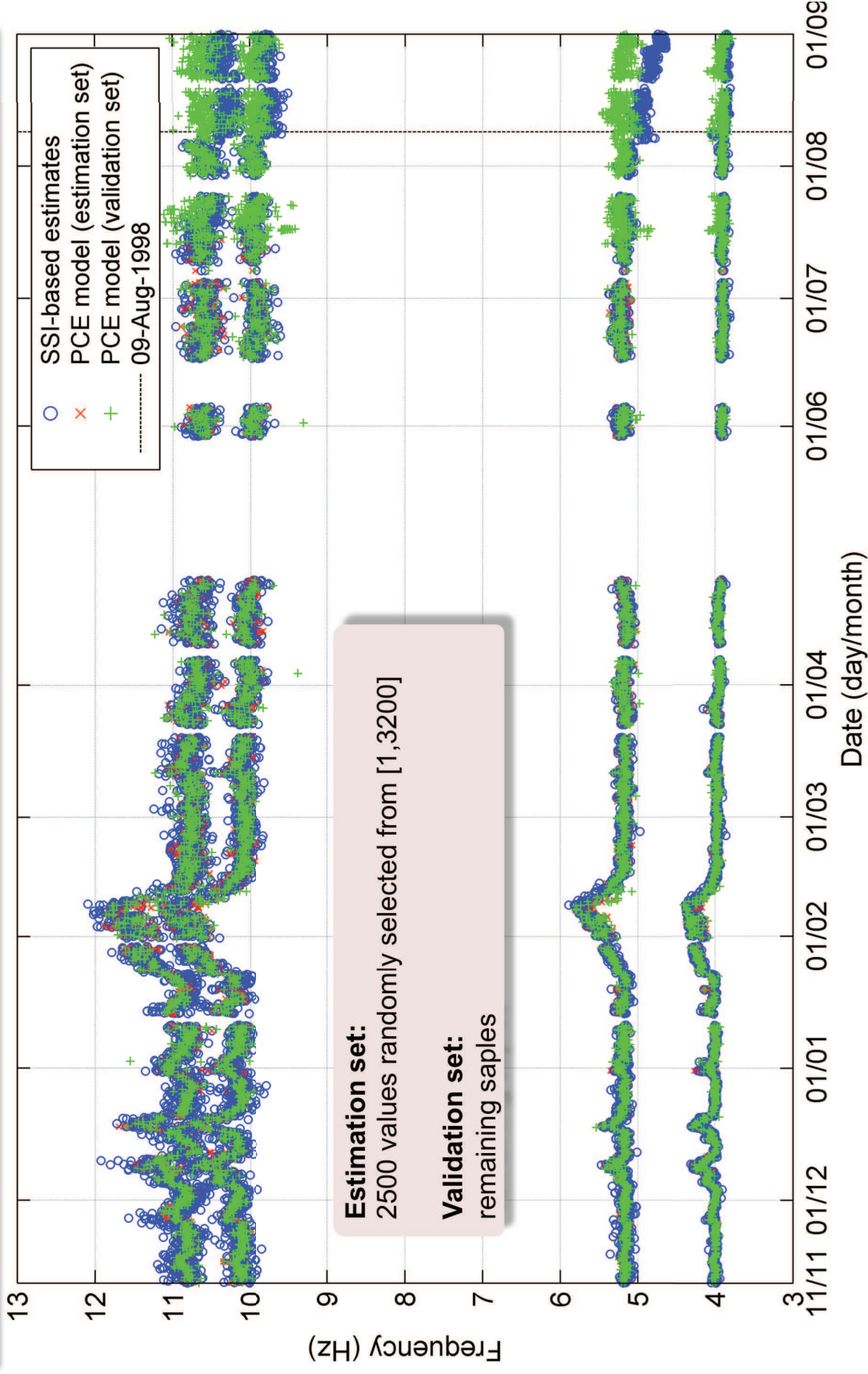
std(PCE error) (Hz)
(estimation set)

0.0275

0.0528

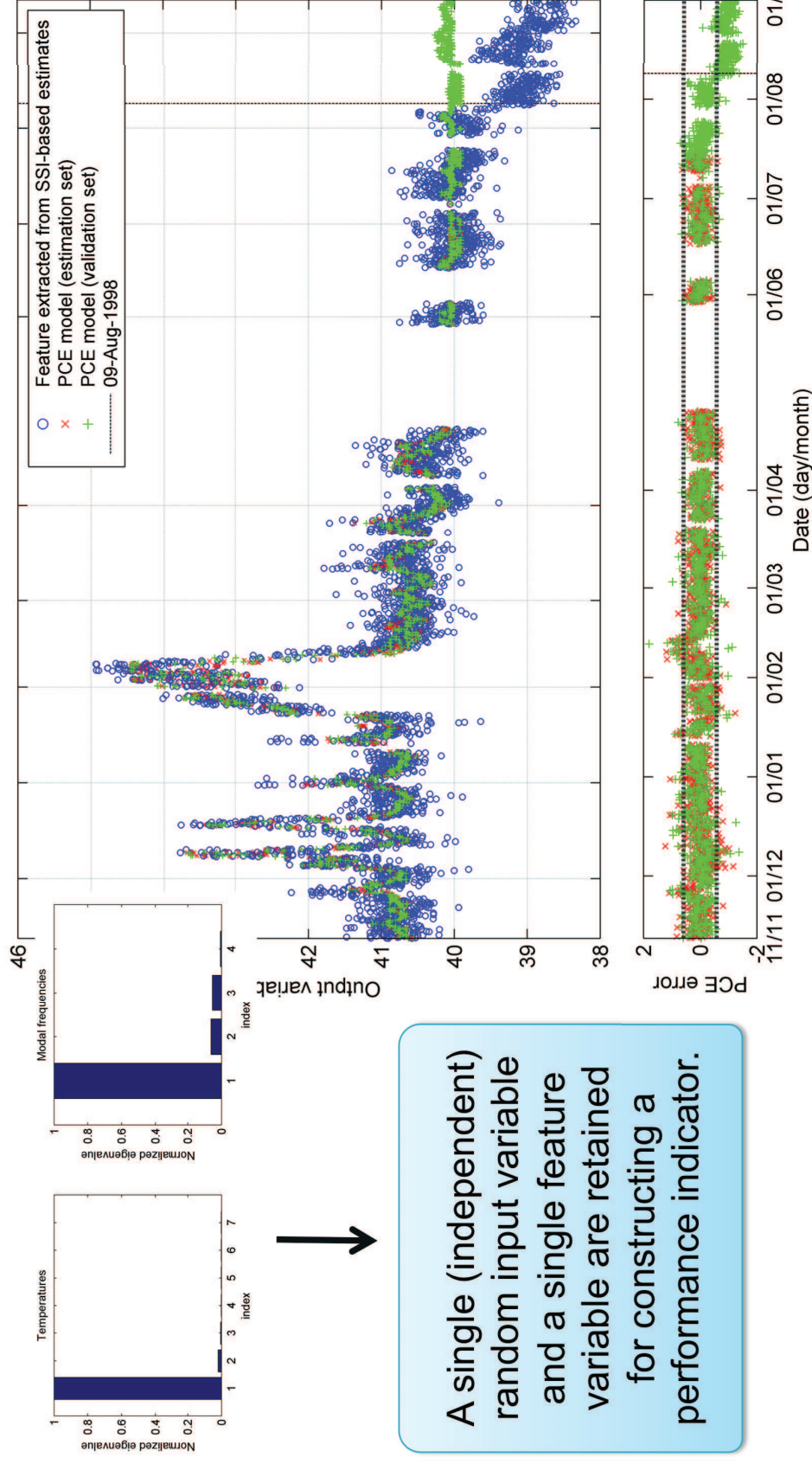
0.1013

0.1313

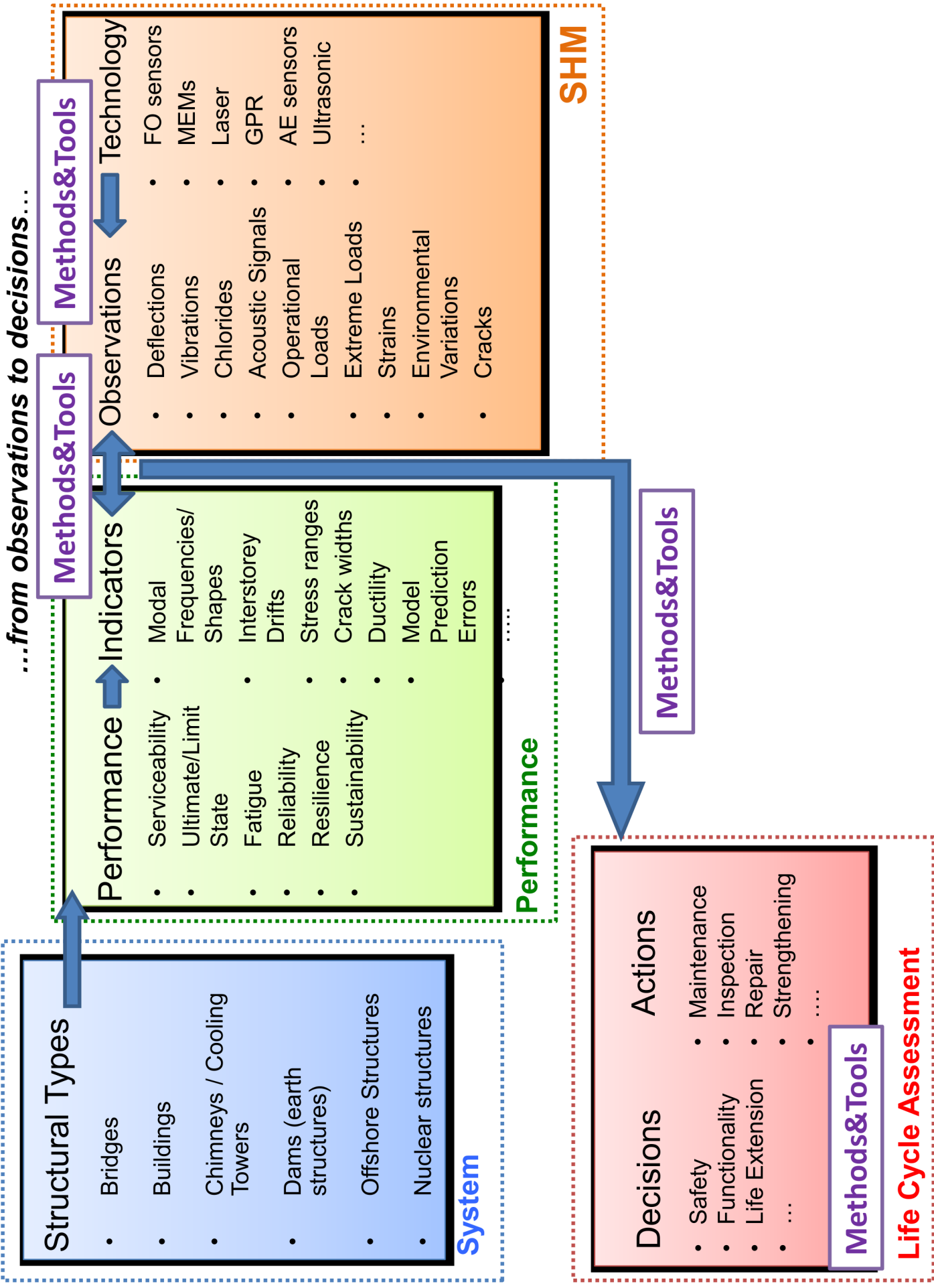


Performance Indicator

An Independent Component Analysis algorithm is utilized for estimating independent random variables from both temperature measurements (input variables) and the estimated natural frequencies (output)



A single (independent) random input variable and a single feature variable are retained for constructing a performance indicator.



From short-term sensing data to modal characteristics

Modal parameter estimation with subspace-based system identification

- Output-only sensor data y_k under unknown ambient excitation
- Identification of system matrices (A, C) of discrete-time state space model from y_k
- Modal parameters are obtained from eigenvalues and eigenvectors of (A, C)

$$\begin{aligned} M\ddot{z} + C\dot{z} + Kz &= \nu \\ y &= L\dot{z} + e \end{aligned}$$



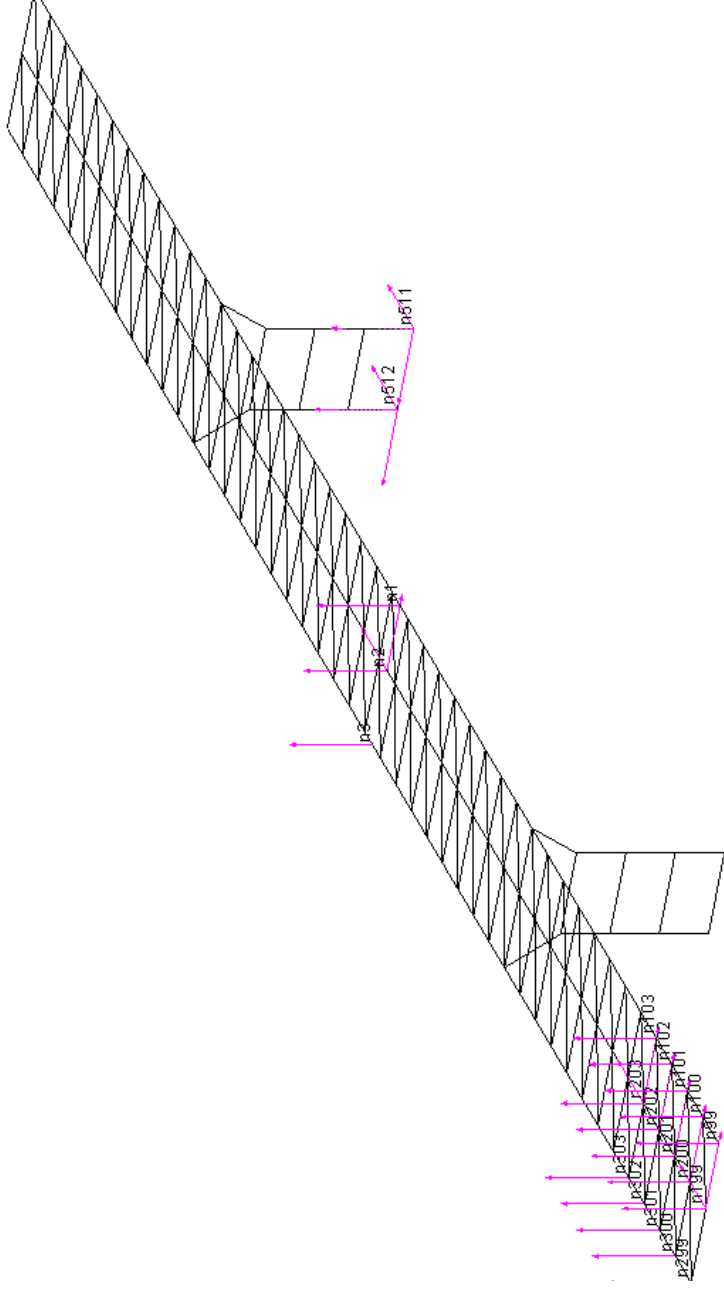
$$\begin{aligned} x_{k+1} &= Ax_k + v_k \\ y_k &= Cx_k + w_k \end{aligned}$$

Methods

- Modal parameter identification from multiple measurement setups with moving and fixed sensors
- Uncertainty quantification of estimates

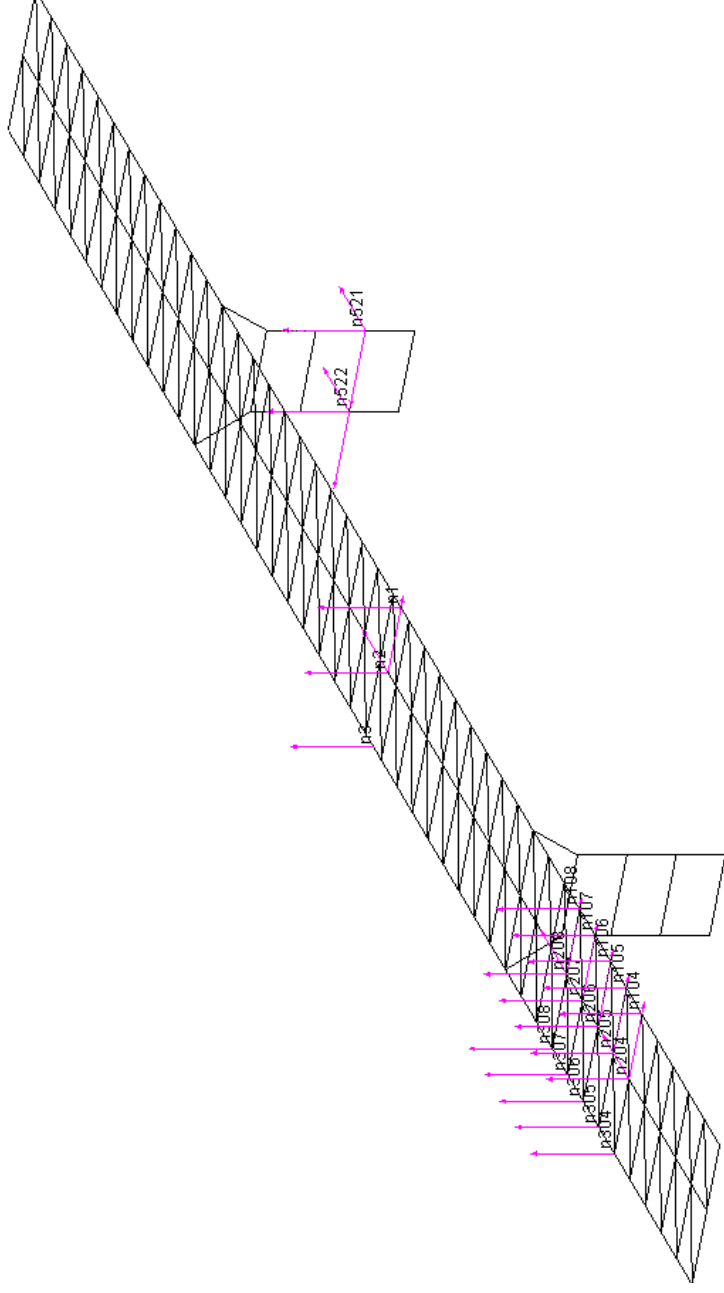
From short-term sensing data to modal characteristics

Sensor configuration in 9 measurement setups



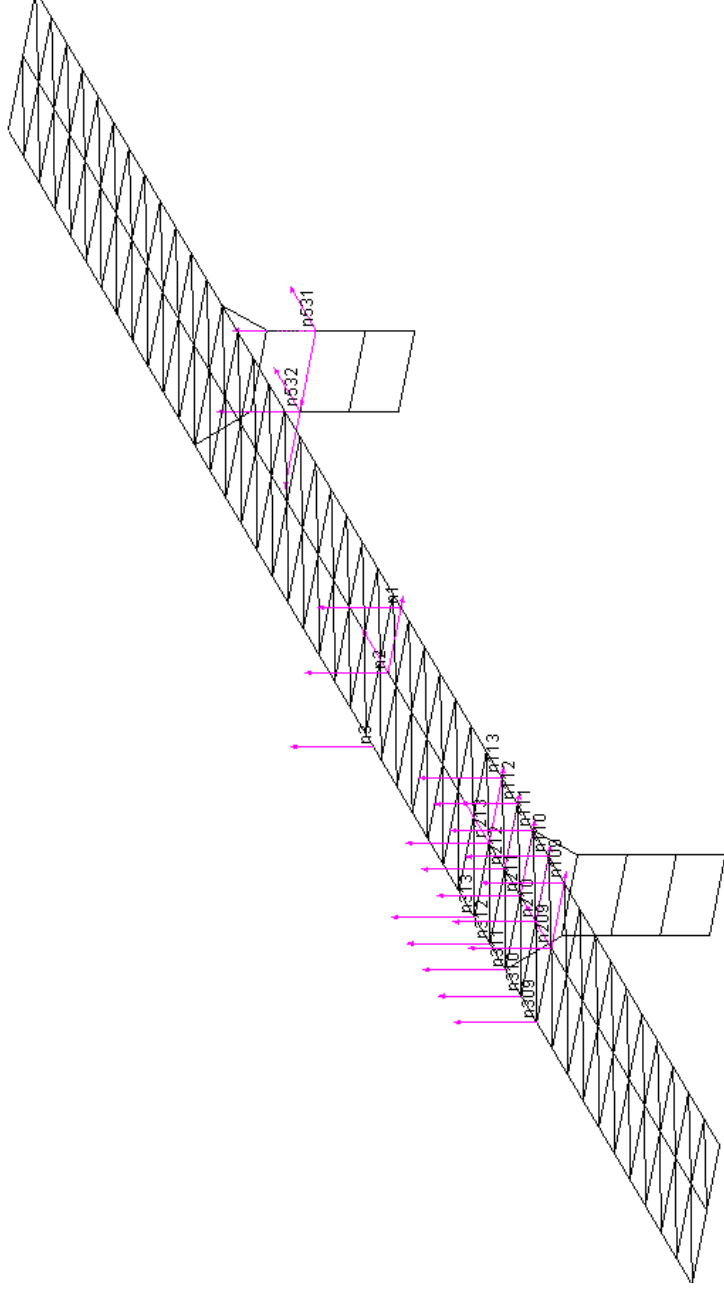
From short-term sensing data to modal characteristics

Sensor configuration in 9 measurement setups



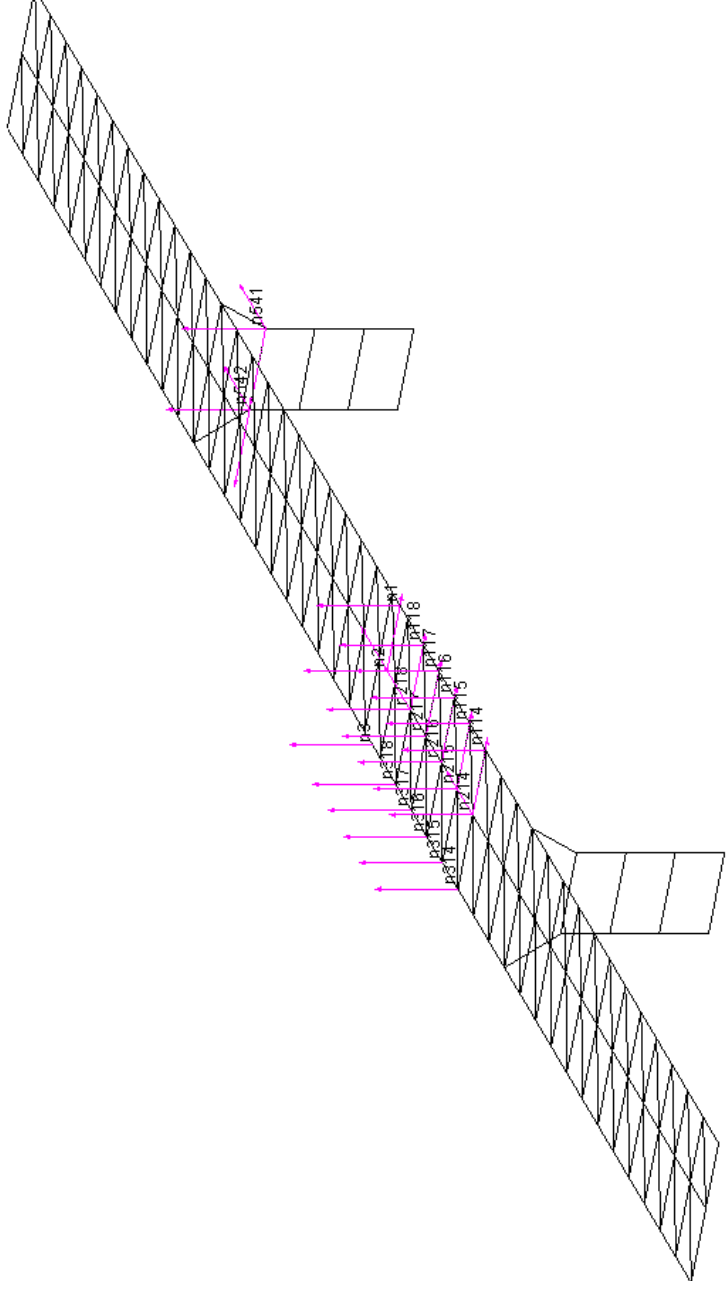
From short-term sensing data to modal characteristics

Sensor configuration in 9 measurement setups



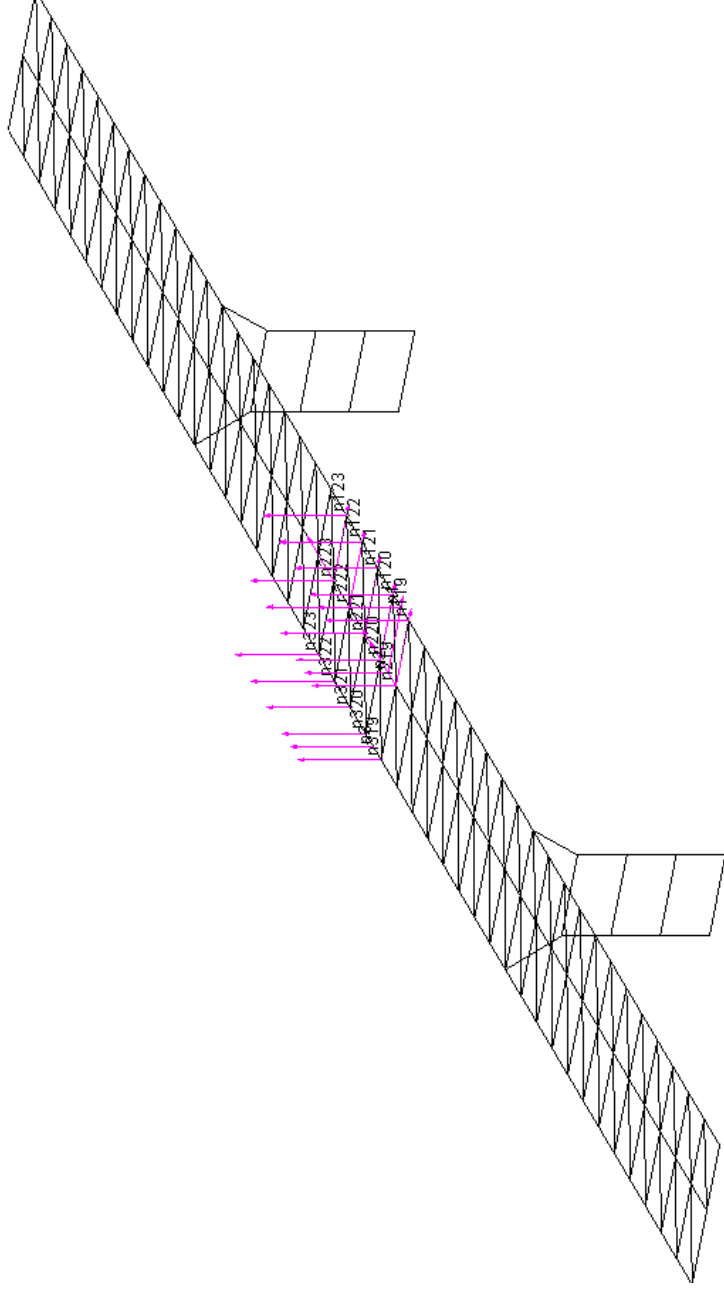
From short-term sensing data to modal characteristics

Sensor configuration in 9 measurement setups



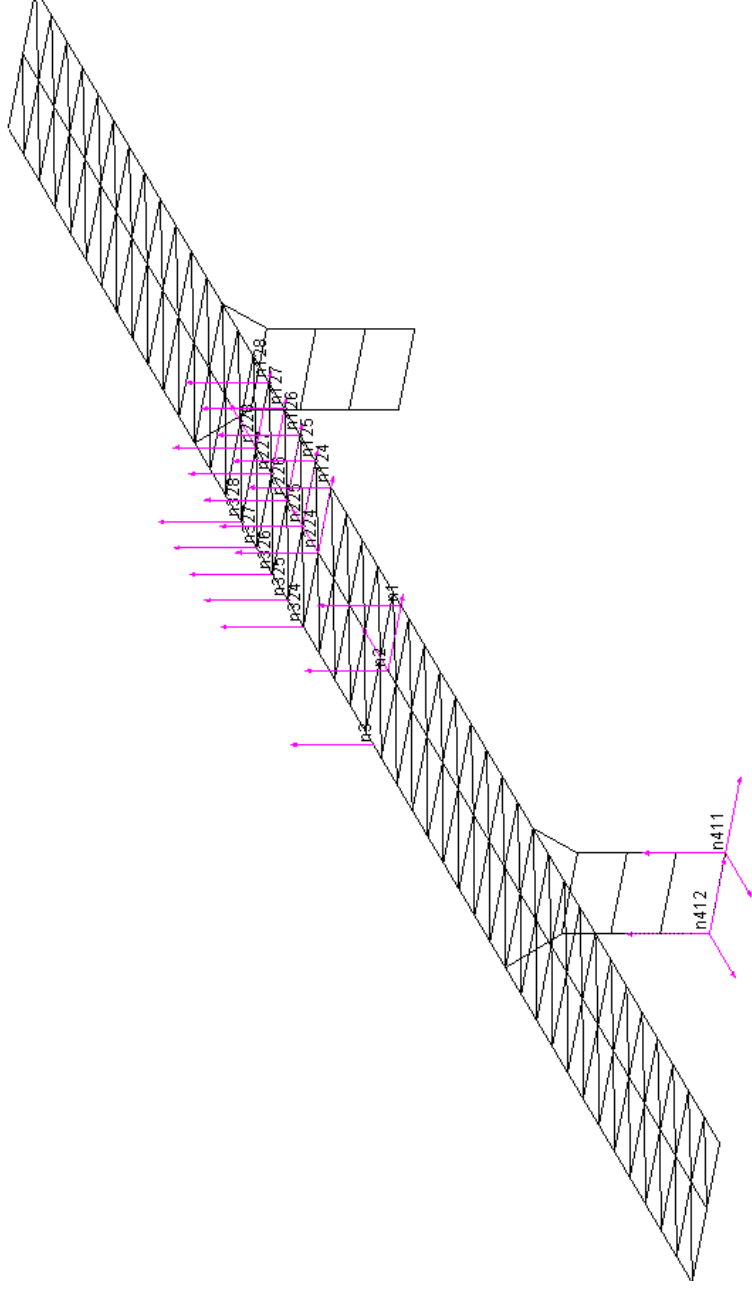
From short-term sensing data to modal characteristics

Sensor configuration in 9 measurement setups



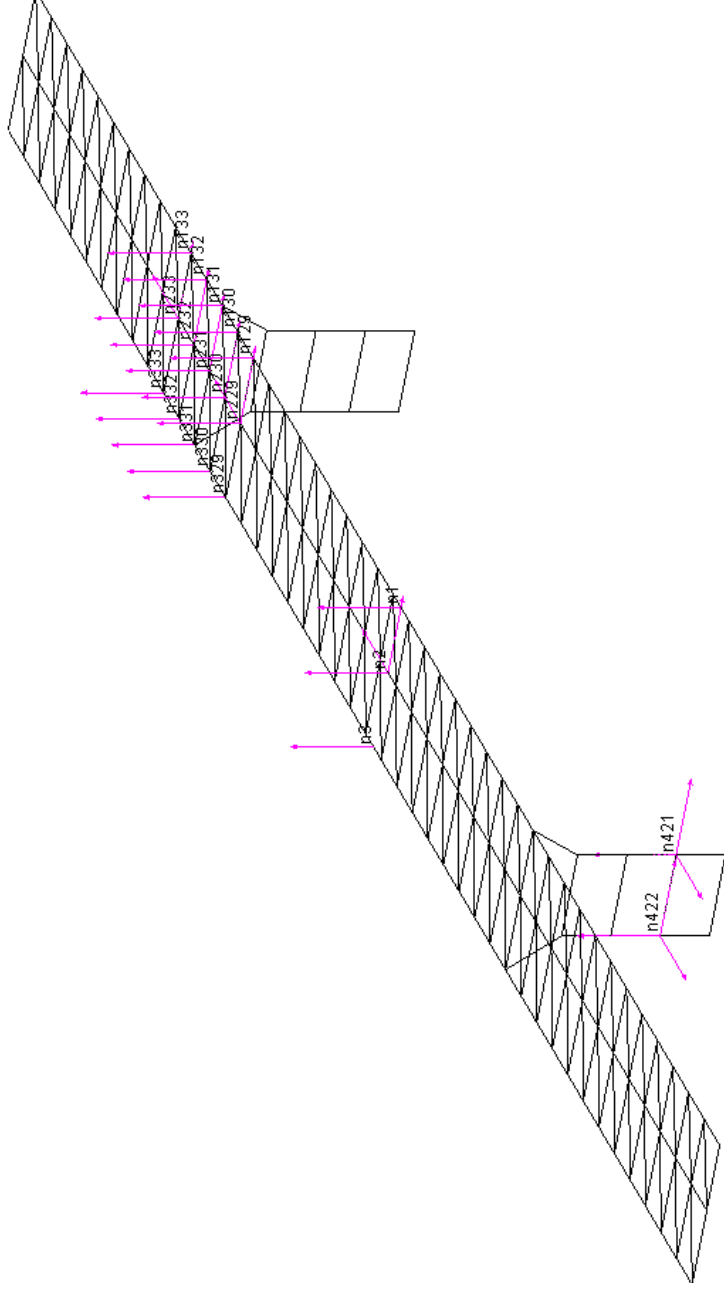
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Sensor configuration in 9 measurement setups



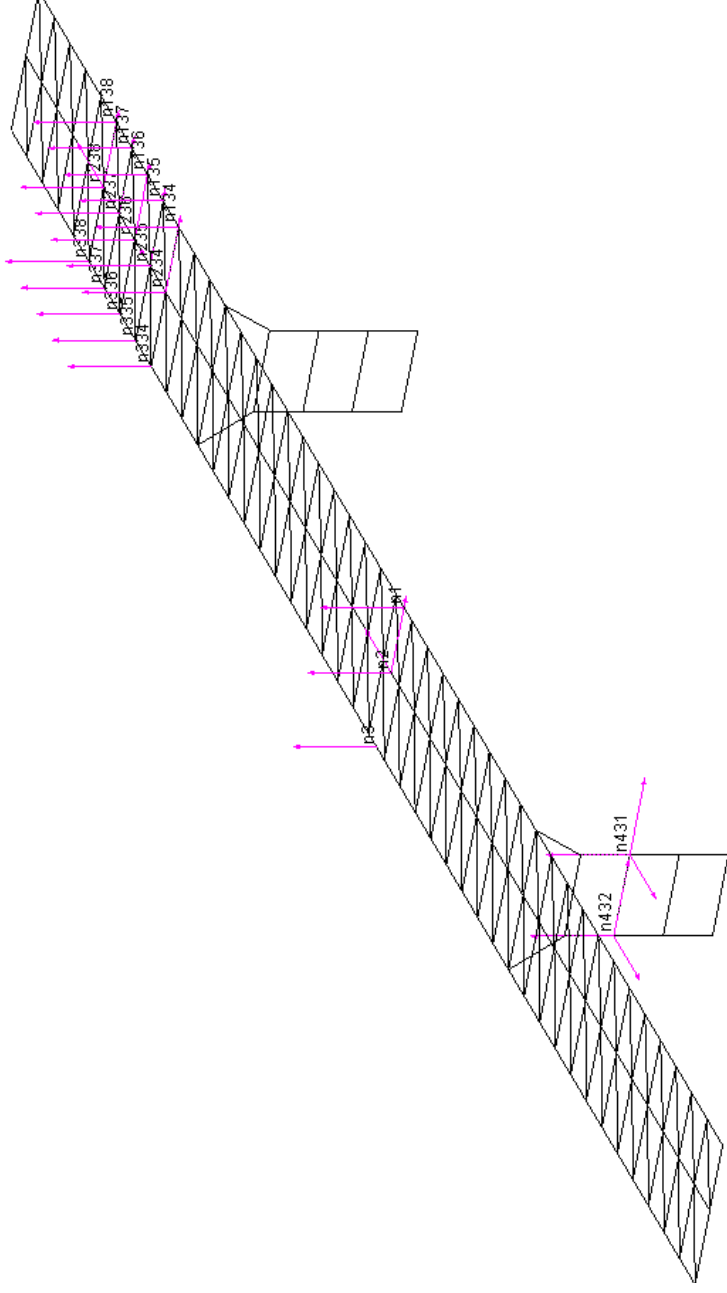
From short-term sensing data to modal characteristics

Sensor configuration in 9 measurement setups



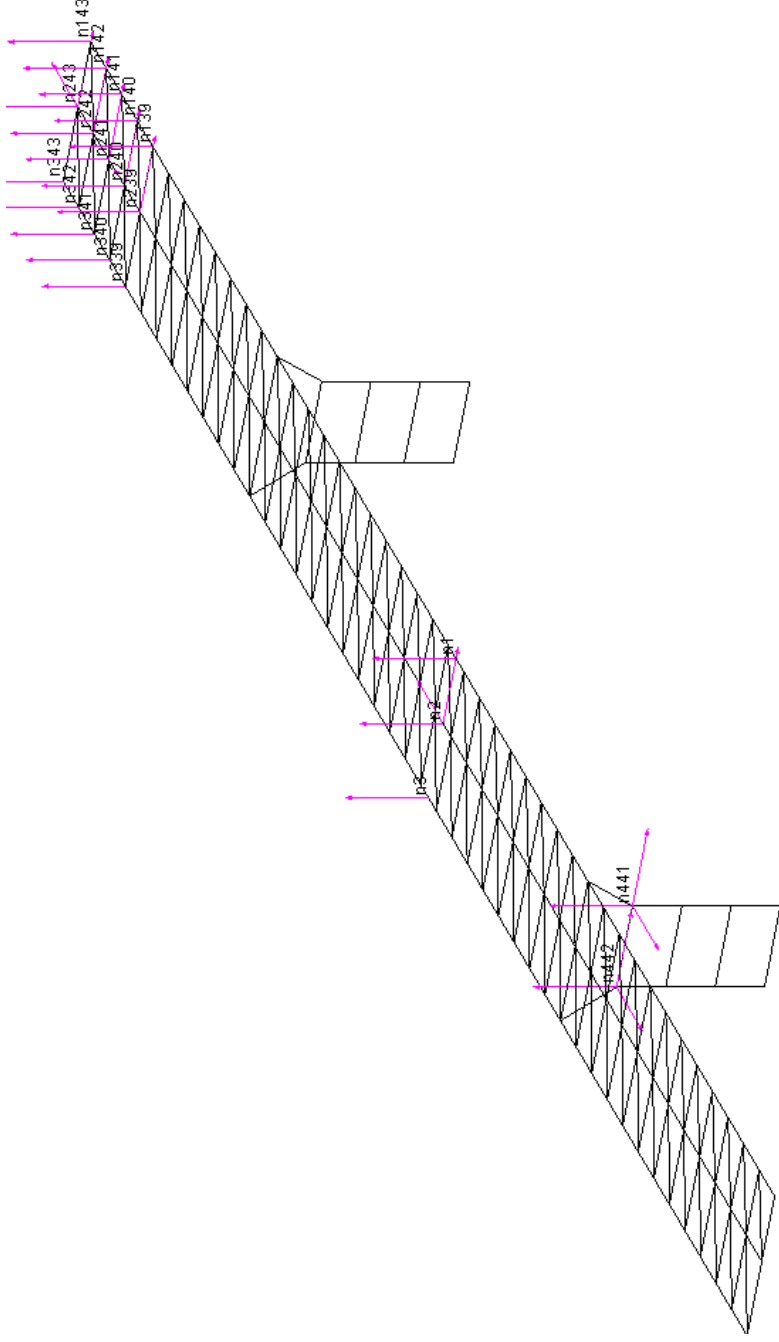
From short-term sensing data to modal characteristics

Sensor configuration in 9 measurement setups



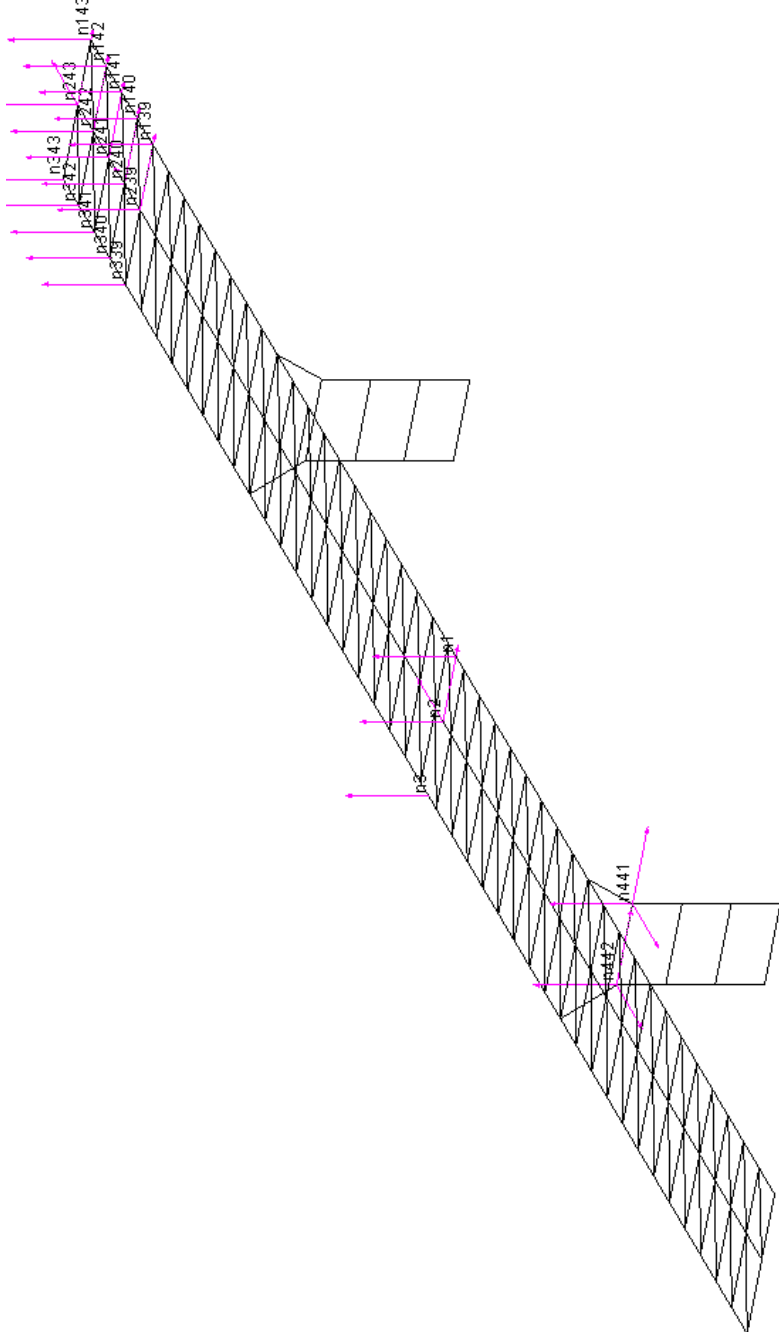
From short-term sensing data to modal characteristics

Sensor configuration in 9 measurement setups



From short-term sensing data to modal characteristics

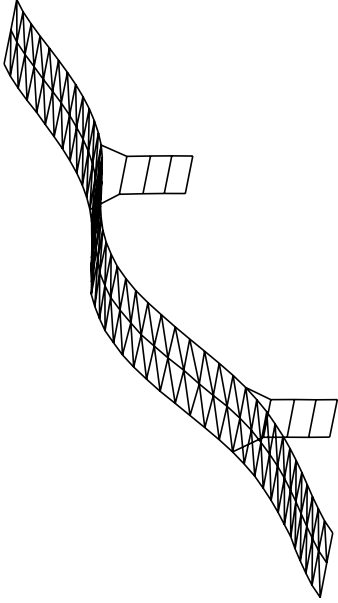
Sensor configuration in 9 measurement setups



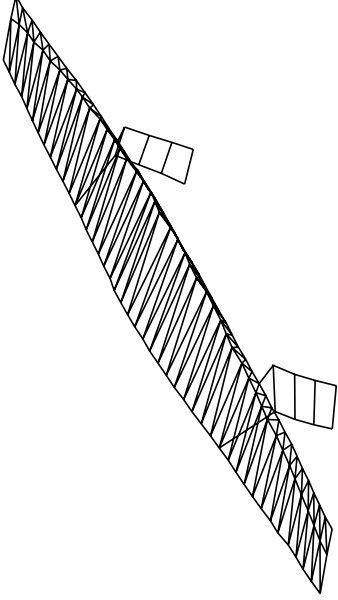
→ “Normalization” of data with respect to fixed sensors and merging for global system identification

Modal parameter estimates

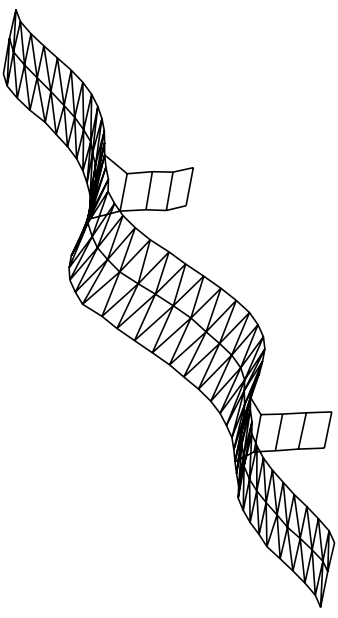
mode 1: 3.86 Hz, 0.6%



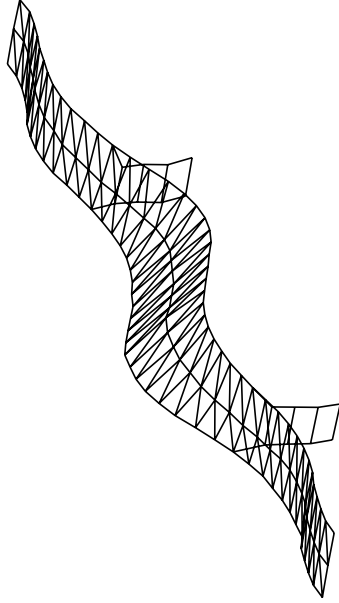
mode 2: 4.88 Hz, 1.4%



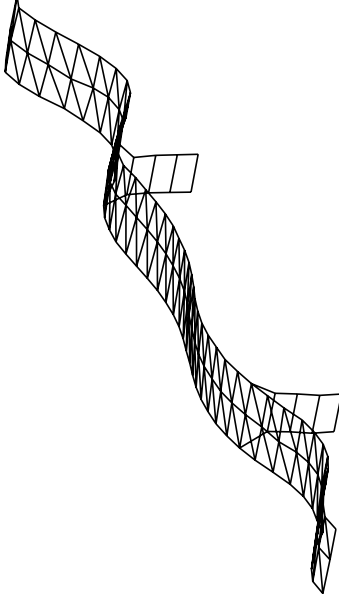
mode 3: 9.79 Hz, 1.4%



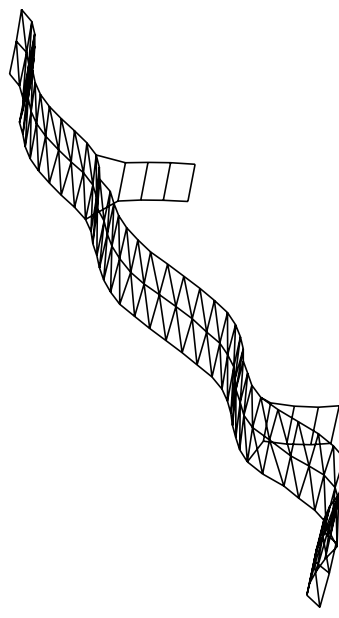
mode 4: 10.3 Hz, 1.9%



mode 5: 12.3 Hz, 3.4%

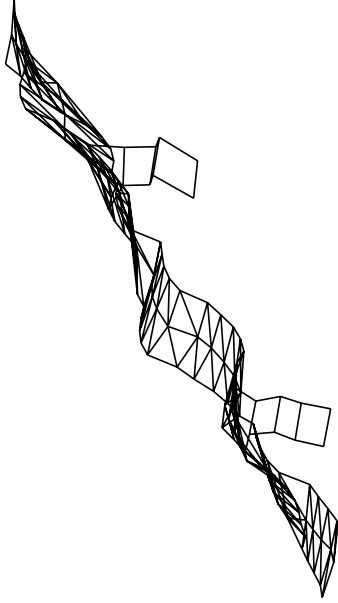


mode 6: 13.3 Hz, 3.5%

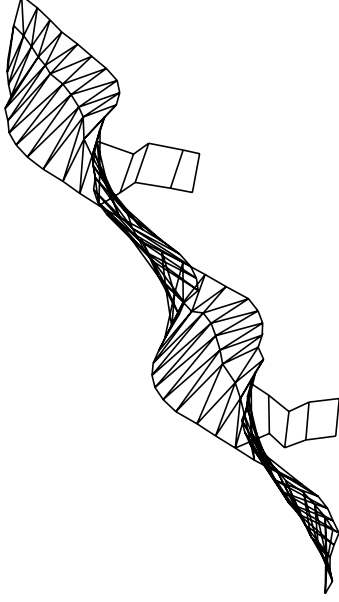


Modal parameter estimates

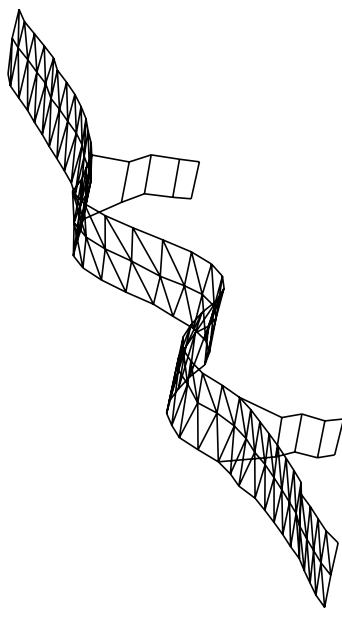
mode 7: 17.2 Hz, 7.2%



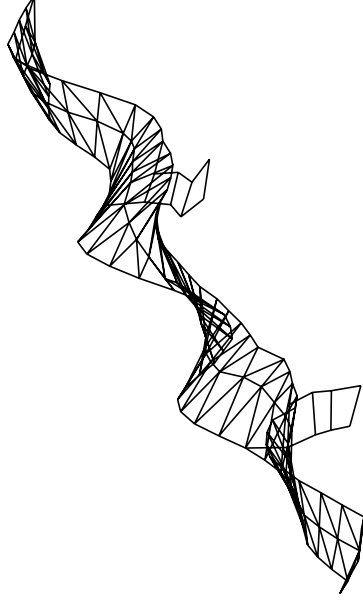
mode 8: 19.2 Hz, 2.8%



mode 9: 19.8 Hz, 4.0%

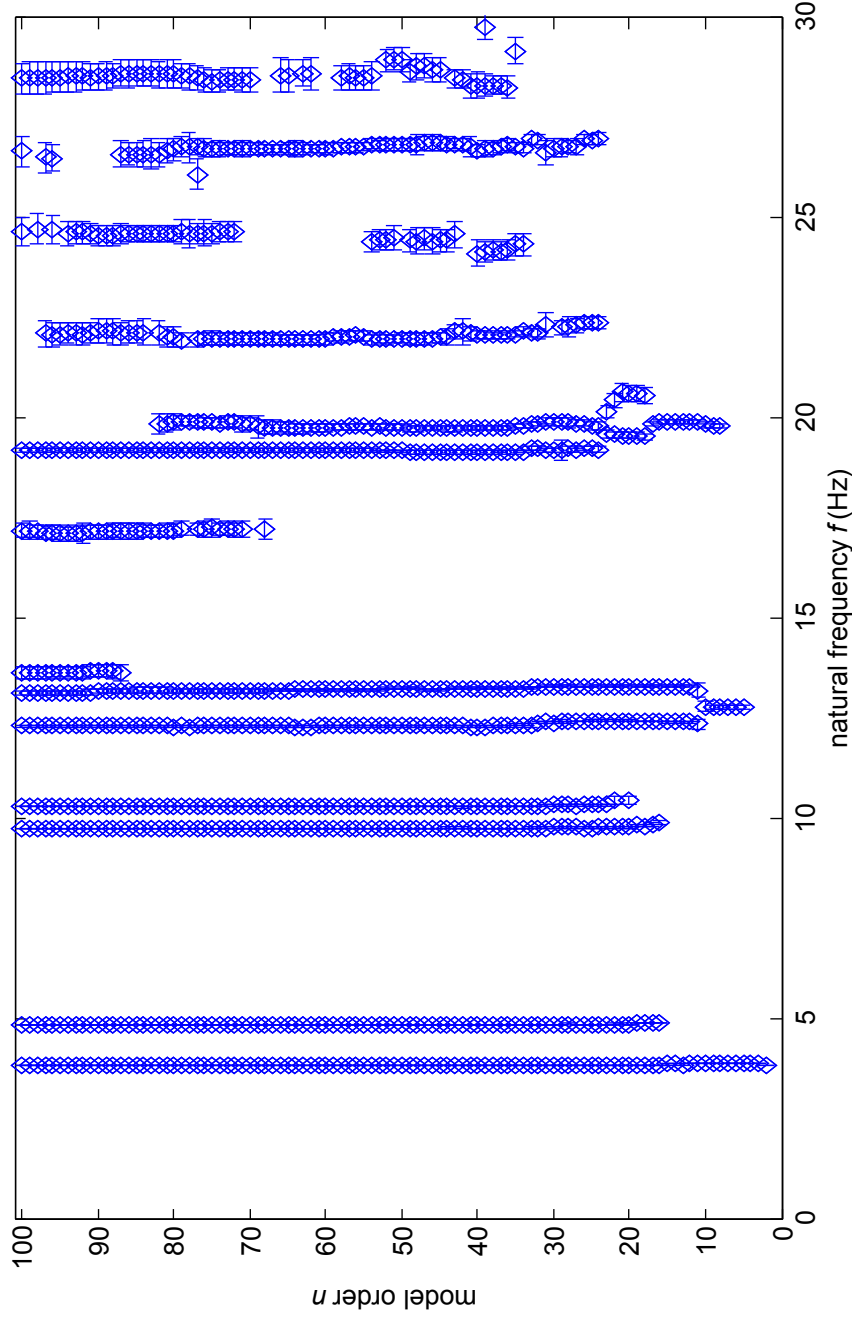


mode 10: 26.8 Hz, 4.9%



Uncertainty quantification

- Sources of uncertainty: unknown inputs, measurement noise, finite data
- Modal parameter estimates are (asymptotically) Gaussian
$$\hat{f} \sim \mathcal{N}(f, \sigma_f^2)$$
- Estimate modal parameter f and its standard deviation σ_f on the same dataset
- Estimates for frequencies, damping ratios and mode shapes



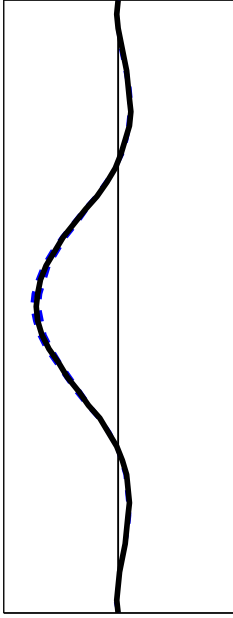
Uncertainty quantification

Identified frequencies and damping ratios with coefficients of variation.

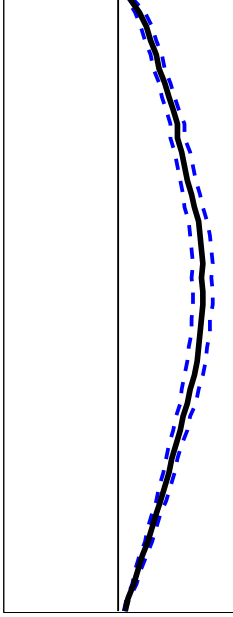
Mode	f_i (Hz)	$100 \sigma_{f_i} / f_i$	ξ_i (%)	$100 \sigma_{\xi_i} / \xi_i$
1	3.864	0.05	0.61	8.8
2	4.883	0.05	1.43	4.7
3	9.787	0.06	1.36	3.6
4	10.32	0.09	1.87	5.4
5	12.33	0.19	3.40	4.9
6	13.27	0.16	3.47	4.3
7	17.20	0.95	7.18	14
8	19.22	0.21	2.83	8.6
9	19.79	0.23	3.97	5.5
10	26.83	0.58	4.86	13

Uncertainty quantification

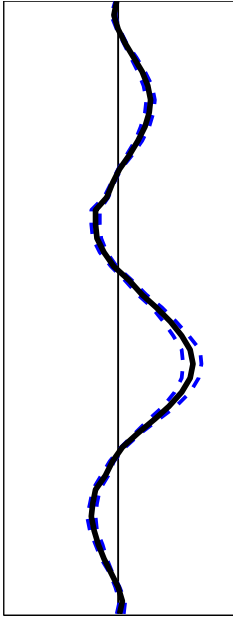
mode 1



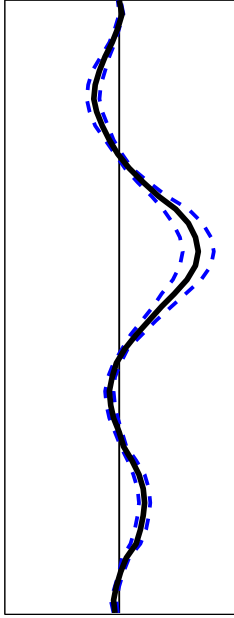
mode 2



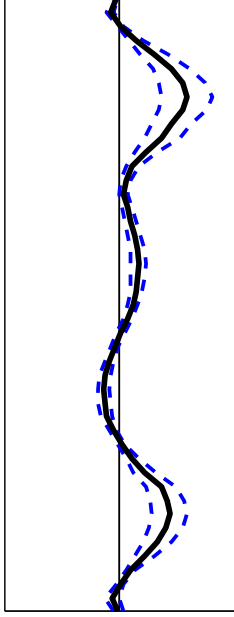
mode 3



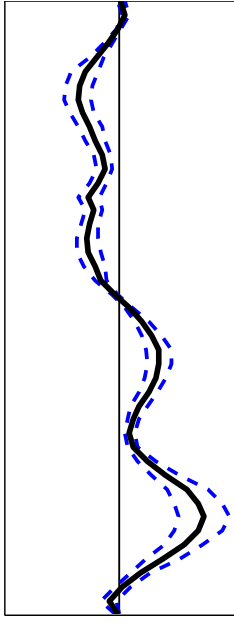
mode 4



mode 5

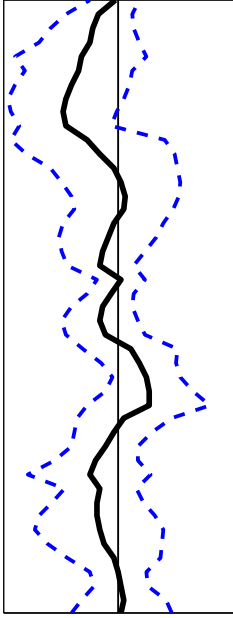


mode 6

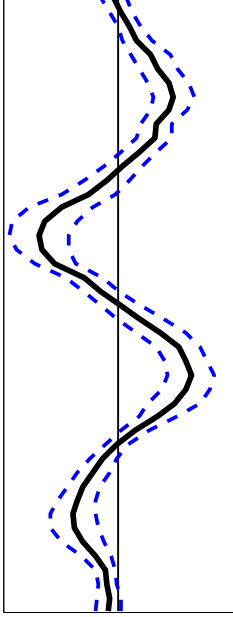


Uncertainty quantification

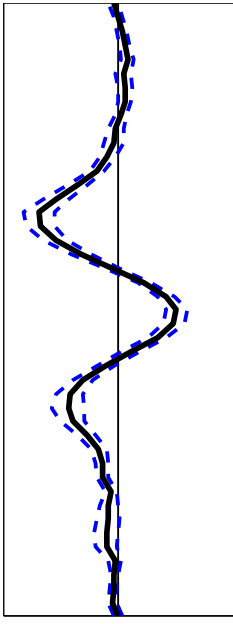
mode 7



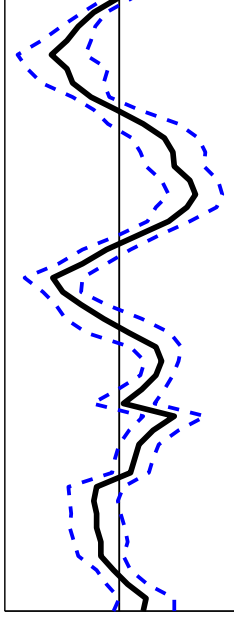
mode 8



mode 9



mode 10



References

Many benchmark results have already been reported by many researchers.

Overviews can be found in

- E. Reynders and G. De Roeck. Vibration-based damage identification: the Z24 benchmark. In M. Beer, I.A. Kougiontzoglou, E. Patelli, and I.S.-K. Au, editors, *Encyclopedia of Earthquake Engineering*. Springer, 2015.
- E. Reynders and G. De Roeck. Continuous vibration monitoring and progressive damage testing on the Z24 bridge. In C. Boller, F.K. Chang, and Y. Fujino, editors, *Encyclopedia of Structural Health Monitoring*, pages 2149-2158. John Wiley & Sons, New York, NY, 2009.
- B. Peeters and C. Ventura. Comparative study of modal analysis techniques for bridge dynamic characteristics. *Mechanical Systems and Signal Processing*, 17(5):965-988, 2003.